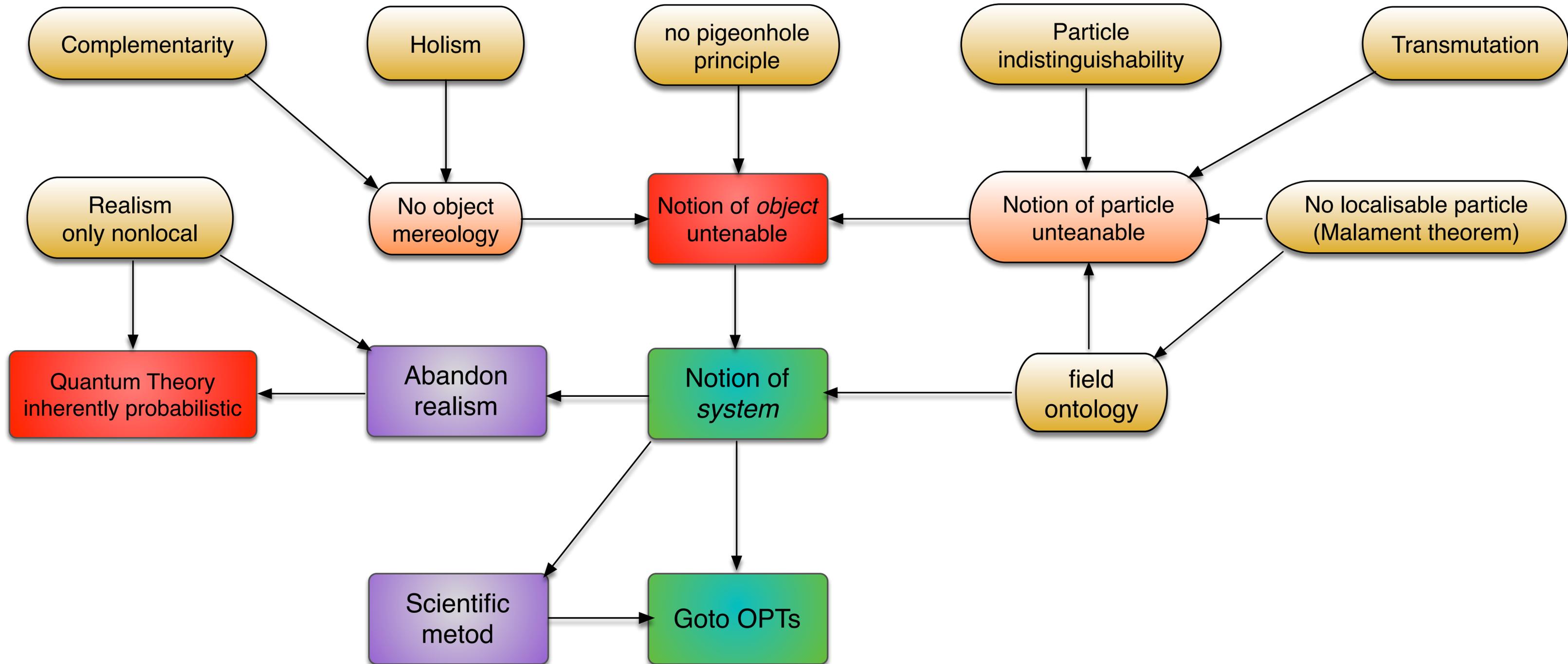


Quantum Theory no unitary ontology, no paradoxes

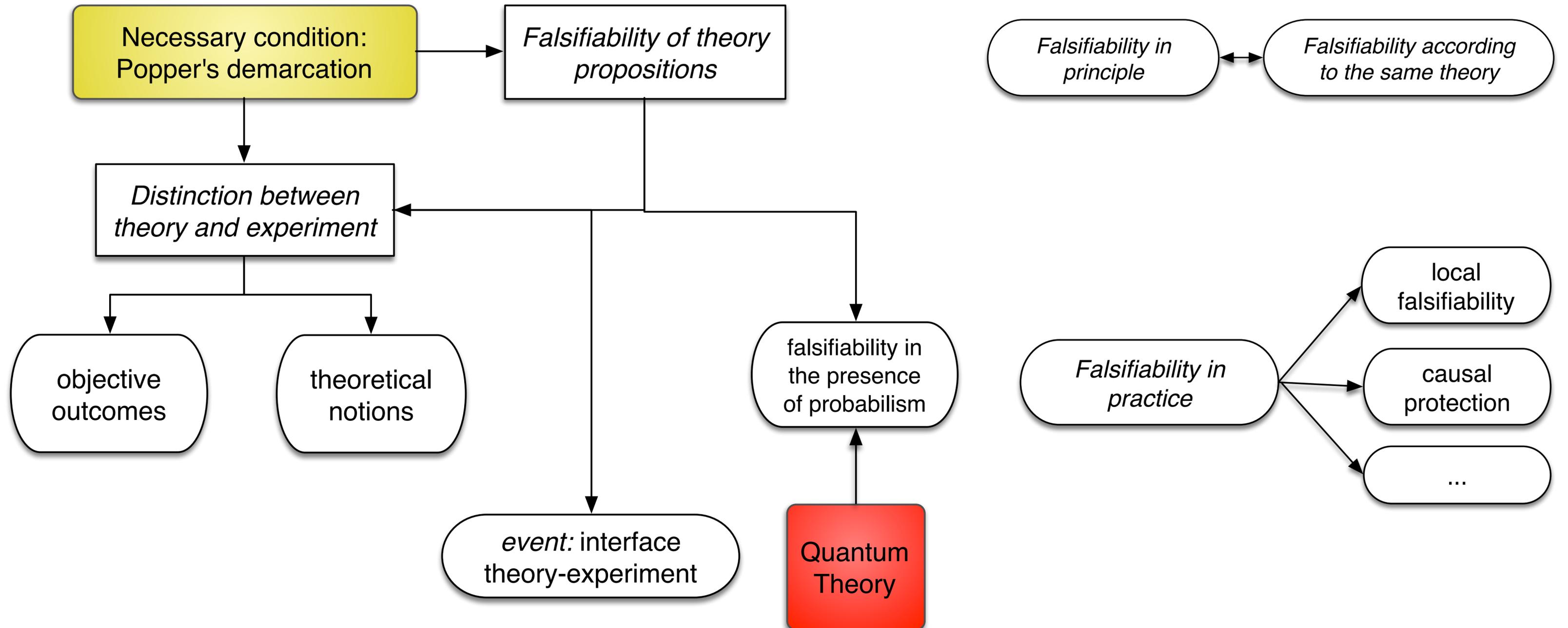
Giacomo Mauro D'Ariano
Università degli Studi di Pavia

New Directions in the Foundations of Physics

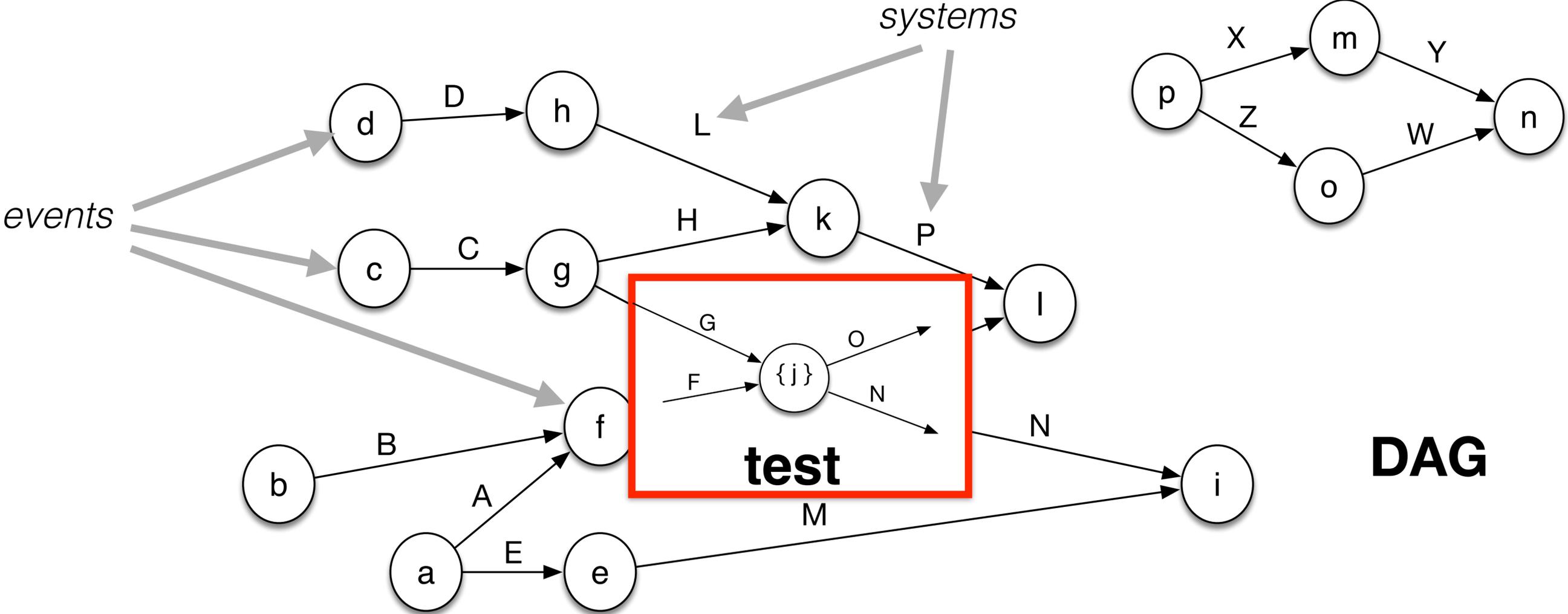
Theoretical notion: “object” \implies “system”



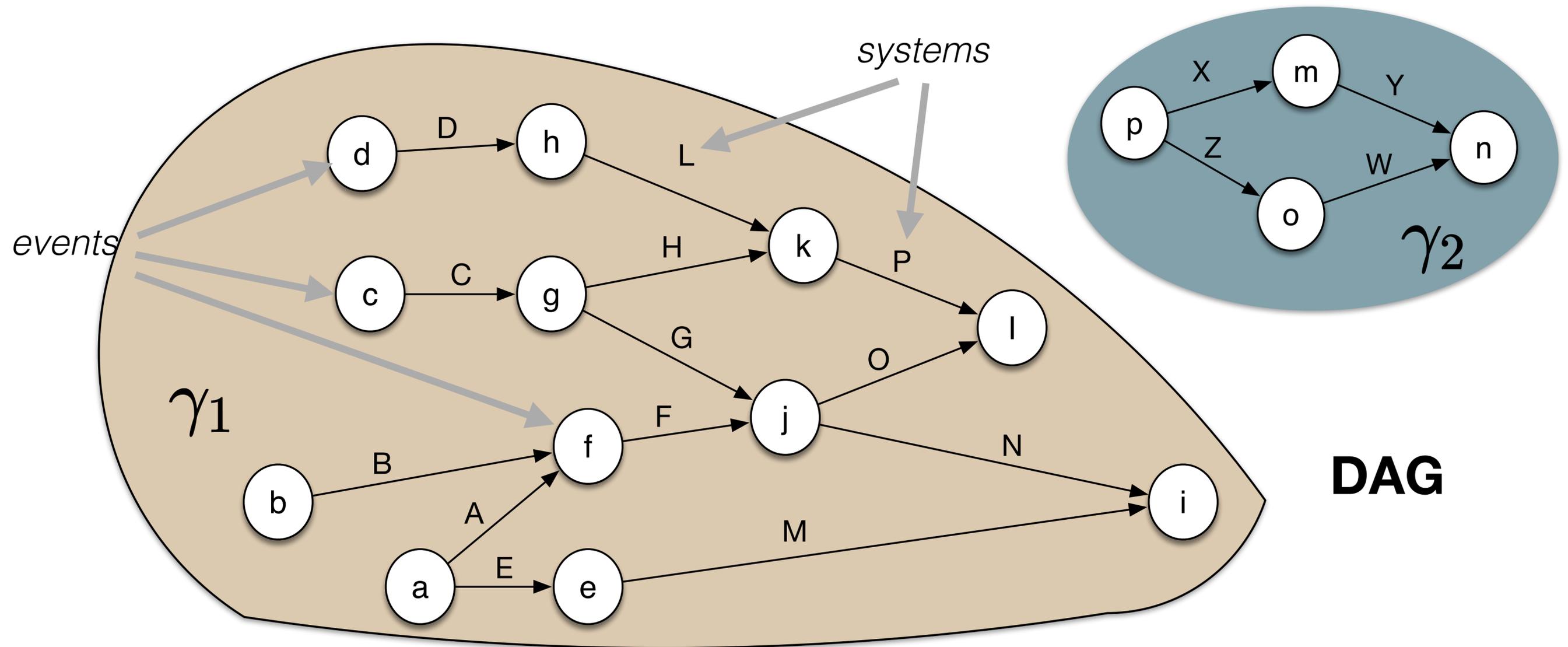
About scientific method



Operational probabilistic theory (OPT)

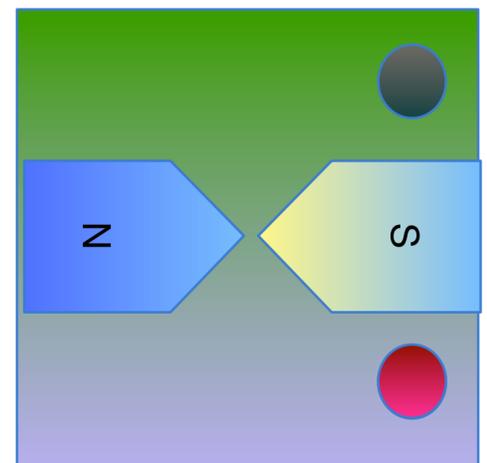
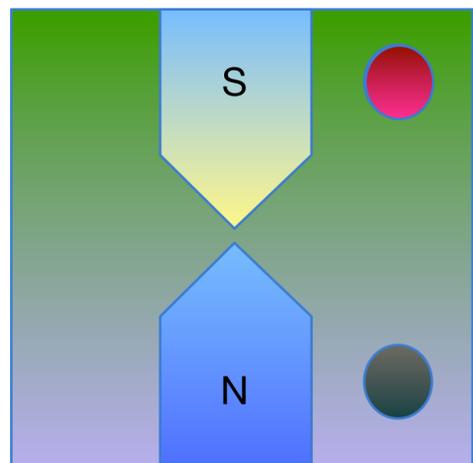
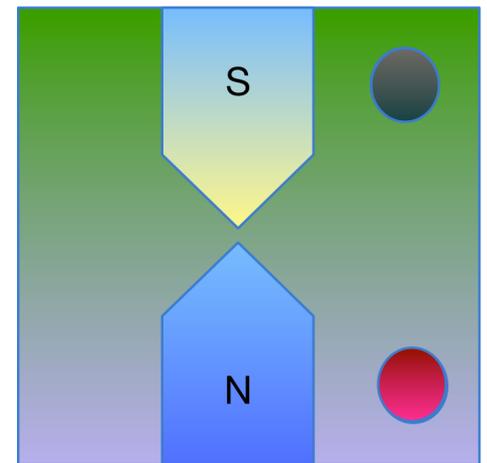
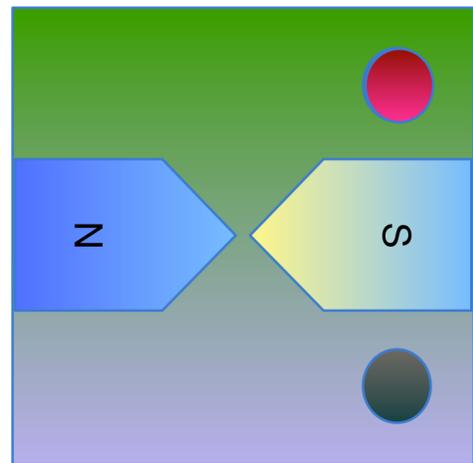
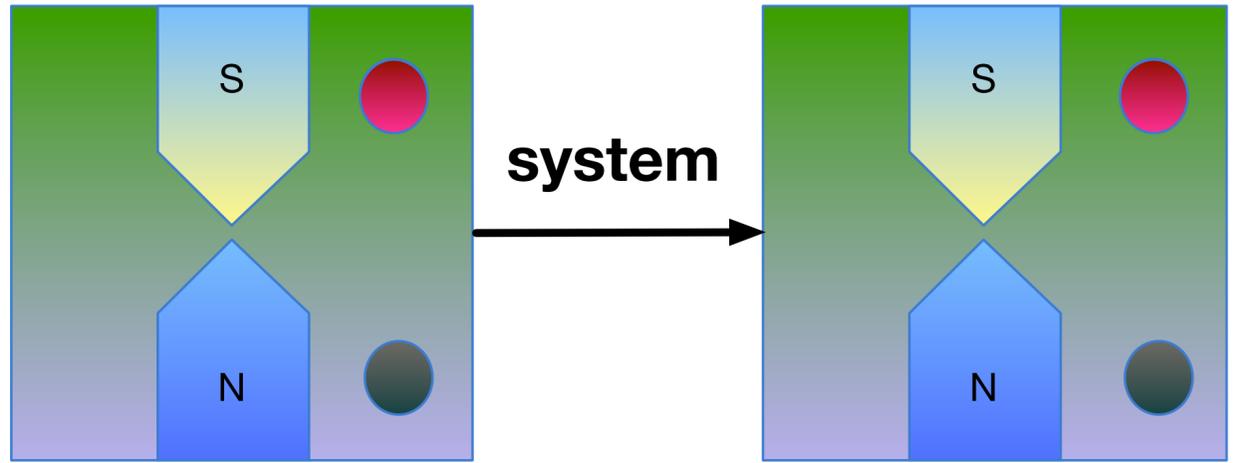


Operational probabilistic theory (OPT)



$$p(abc, \dots, o | \gamma_1 \cup \gamma_2) = p(abc, \dots, l | \gamma_1) p(n, \dots, p | \gamma_2)$$

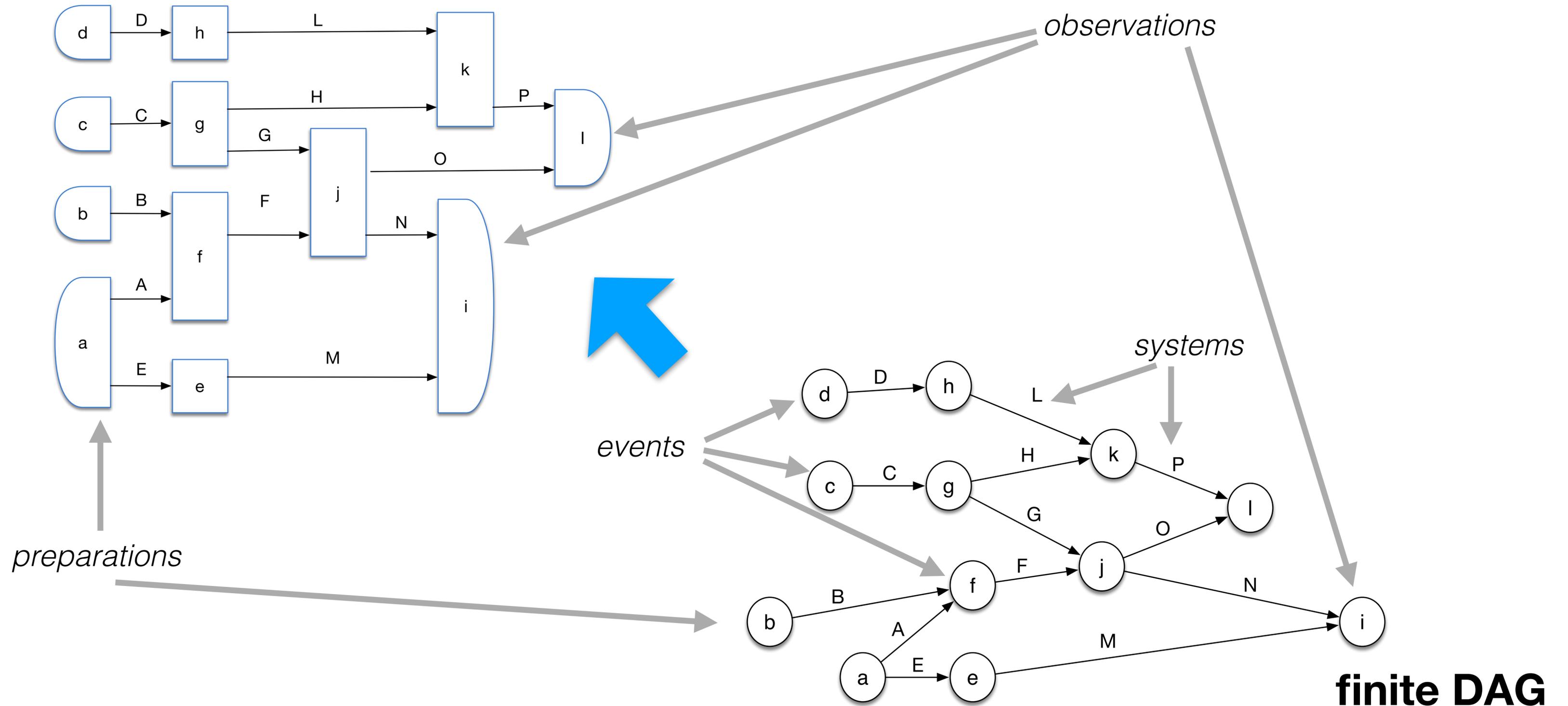
NOTICE: marginals depend on the marginalised part of the graph!



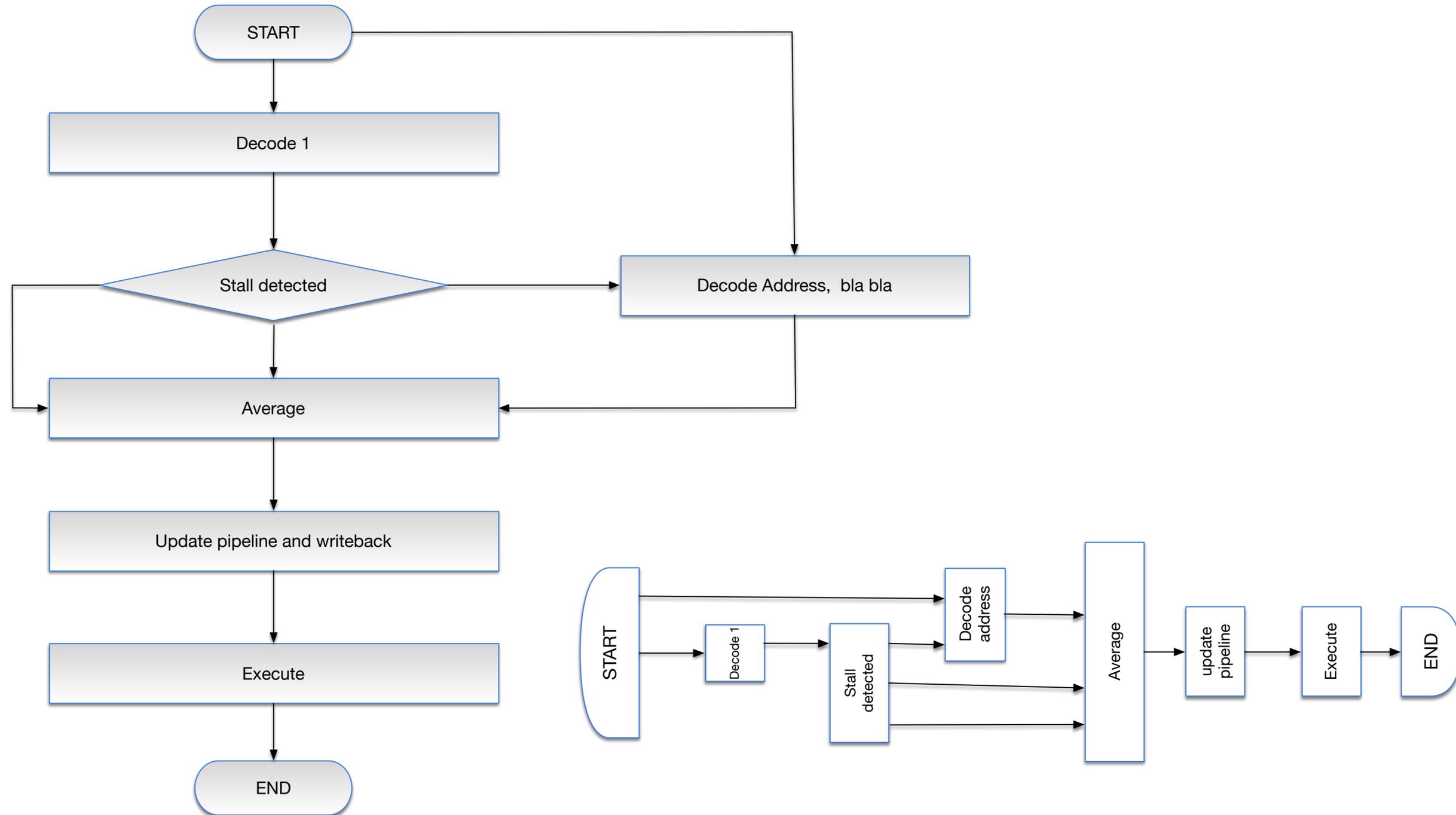
Quantum Theory: the “grammar” of Physics

Quantum Theory is an OPT

An OPT is an Information Theory



An OPT is an Information Theory



OPT framework

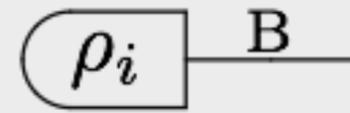
joint probabilities + **connectivity**



Probabilistic
equivalence classes

category theory:
transformations \rightarrow morphisms
systems \rightarrow objects

OPT: strict monoidal braided category

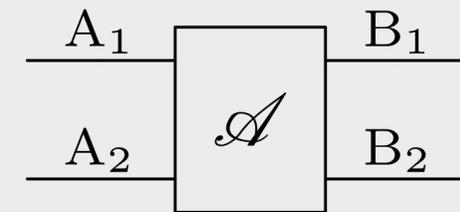


state

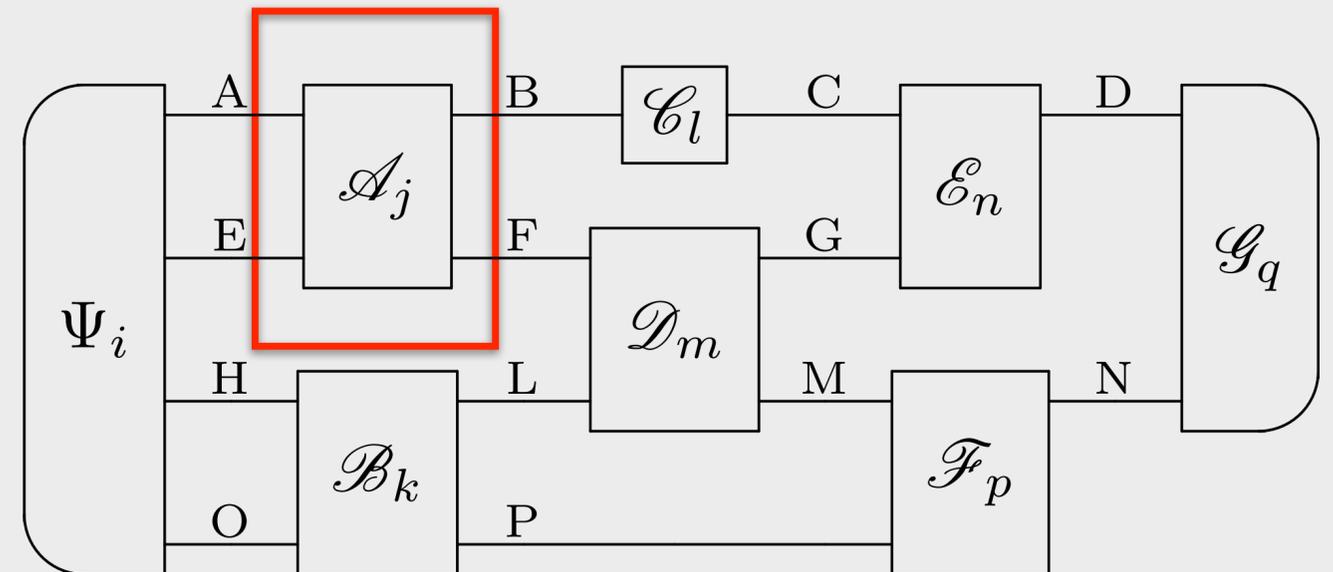


effect

transformation



$p(i, j, k, l, m, n, p, q | \text{circuit})$



OPT framework

Sequential composition (associative)

$$\begin{array}{c}
 \text{---} \overset{A}{\text{---}} \boxed{\{\mathcal{A}_x\}_{x \in X}} \text{---} \overset{B}{\text{---}} \boxed{\{\mathcal{B}_y\}_{y \in Y}} \text{---} \overset{C}{\text{---}} \quad =: \quad \text{---} \overset{A}{\text{---}} \boxed{\{\mathcal{B}_x \circ \mathcal{A}_y\}_{(x,y) \in X \times Y}} \text{---} \overset{C}{\text{---}}
 \end{array}$$

Identity test

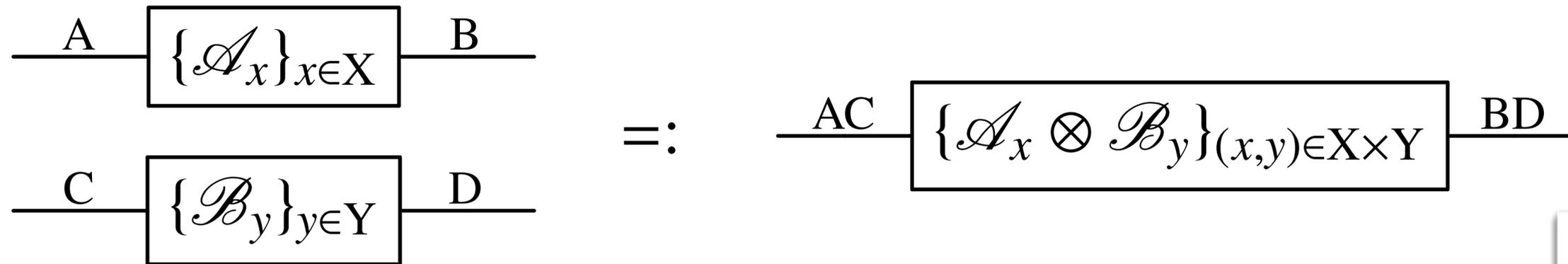
$$\begin{array}{c}
 \text{---} \overset{A}{\text{---}} \boxed{\mathcal{I}_A} \text{---} \overset{A}{\text{---}} \boxed{\mathcal{C}} \text{---} \overset{B}{\text{---}} \quad = \quad \text{---} \overset{A}{\text{---}} \boxed{\mathcal{C}} \text{---} \overset{B}{\text{---}} \quad = \quad \text{---} \overset{A}{\text{---}} \boxed{\mathcal{C}} \text{---} \overset{B}{\text{---}} \\
 \text{---} \overset{A}{\text{---}} \boxed{\mathcal{D}} \text{---} \overset{B}{\text{---}} \boxed{\mathcal{I}_B} \text{---} \overset{B}{\text{---}} \quad = \quad \text{---} \overset{A}{\text{---}} \boxed{\mathcal{D}} \text{---} \overset{B}{\text{---}} \quad = \quad \text{---} \overset{A}{\text{---}} \boxed{\mathcal{D}} \text{---} \overset{B}{\text{---}}
 \end{array}$$

OPT framework

OPT: strict monoidal braided category

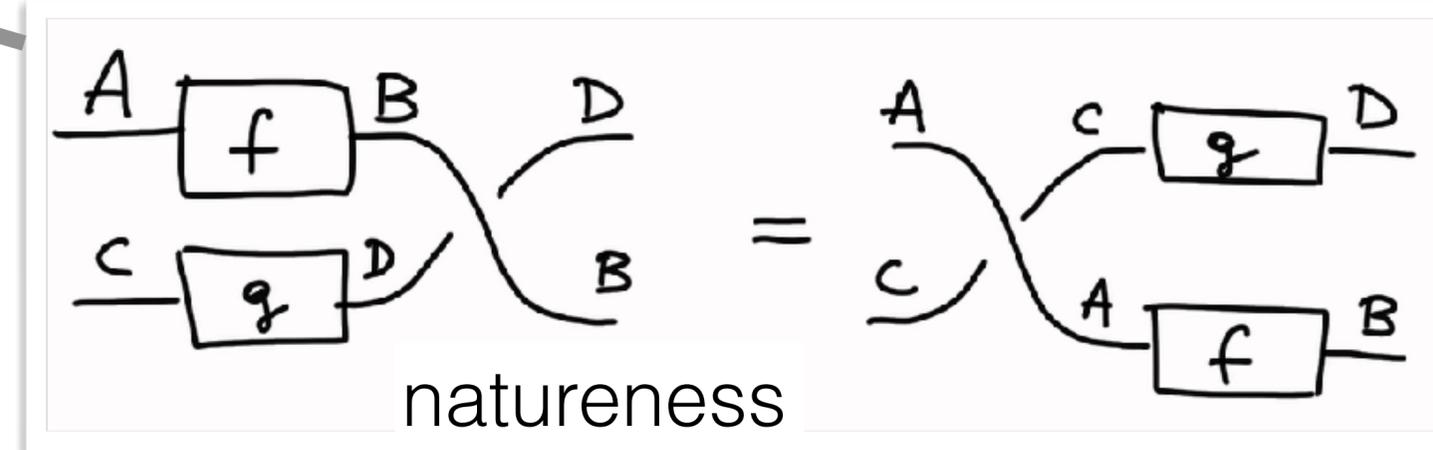
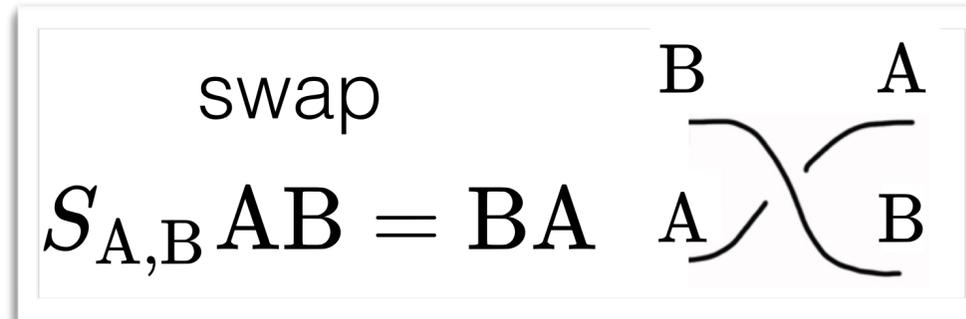
Quantum Theory: symmetric OPT

Parallel composition (associative)



$$AB \simeq BA =: S_{A,B} AB \quad (\text{braided})$$

$$\left. \begin{aligned} AI &= IA \\ A(BC) &= A(BC) \end{aligned} \right\} \quad (\text{strict monoidal})$$

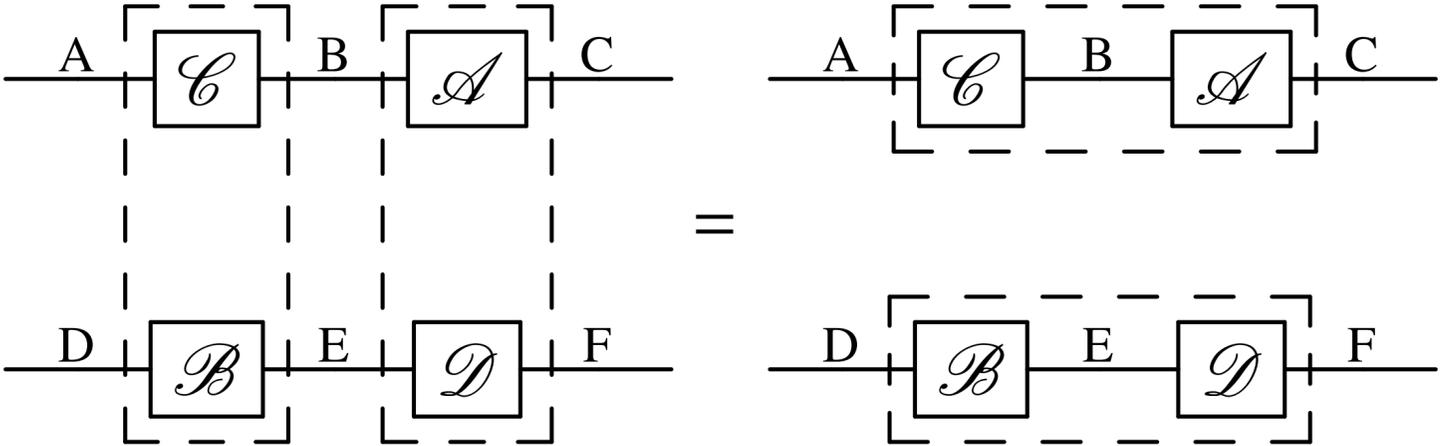


$$(AB)C \simeq A(BC) \quad (\text{monoidal})$$

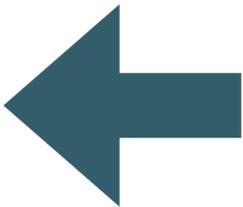
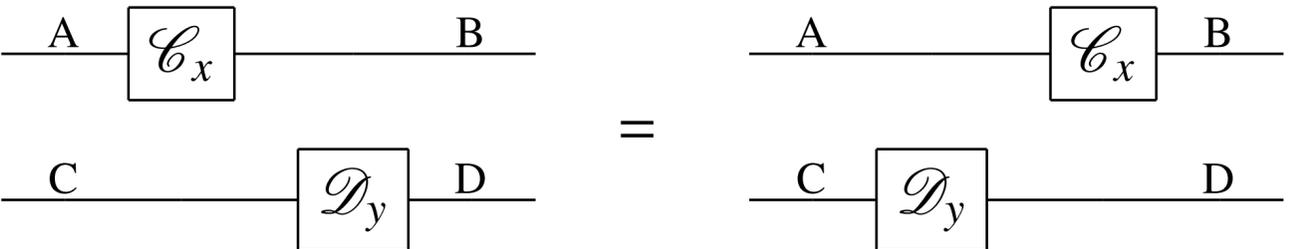
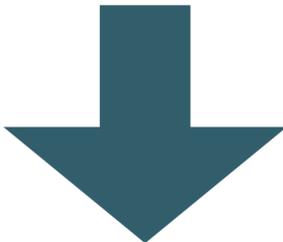
$$S_{A,B}^{-1} = S_{B,A} \quad (\text{symmetric})$$

OPT framework

Sequential and parallel compositions commute



$$(\mathcal{A} \otimes \mathcal{D}) \circ (\mathcal{C} \otimes \mathcal{B}) = (\mathcal{A} \circ \mathcal{C}) \otimes (\mathcal{D} \circ \mathcal{B})$$



wire-stretching
(foliations)

Quantum Theory as OPT

system	A	\mathcal{H}_A	(1)
system composition	AB	$\mathcal{H}_{AB} = \mathcal{H}_A \otimes \mathcal{H}_B$	
transformation	$\mathcal{T} \in \text{Transf}(A \rightarrow B)$	$\mathcal{T} \in \text{CP}_{\leq}(\mathbf{T}(\mathcal{H}_A) \rightarrow \mathbf{T}(\mathcal{H}_B))$	(2)

Theorems

trivial system system	I	$\mathcal{H}_I = \mathbb{C}$	
deterministic transformation	$\mathcal{T} \in \text{Transf}_1(A \rightarrow B)$	$\mathcal{T} \in \text{CP}_{=}(\mathbf{T}(\mathcal{H}_A) \rightarrow \mathbf{T}(\mathcal{H}_B))$	(2)
states	$\rho \in \text{St}(A) \equiv \text{Transf}(I \rightarrow A)$	$\rho \in \mathbf{T}_{\leq 1}^+(\mathcal{H}_A)$	(3)
	$\rho \in \text{St}_1(A) \equiv \text{Transf}_1(I \rightarrow A)$	$\rho \in \mathbf{T}_{=1}^+(\mathcal{H}_A)$	(3)
	$\rho \in \text{St}(I) \equiv \text{Transf}(I \rightarrow I)$	$\rho \in [0, 1]$	
	$\rho \in \text{St}_1(I) \equiv \text{Transf}(I \rightarrow I)$	$\rho = 1$	
effects	$\varepsilon \in \text{Eff}(A) \equiv \text{Transf}(A \rightarrow I)$	$\varepsilon(\cdot) = \text{Tr}_A[\cdot E], 0 \leq E \leq I_A$	(4)
	$\varepsilon \in \text{Eff}_1(A) \equiv \text{Transf}_1(A \rightarrow I)$	$\varepsilon = \text{Tr}_A$	(4)

D'ARIANO,
CHIRIBELLA
AND PERINOTTI



QUANTUM THEORY
FROM FIRST PRINCIPLES

QUANTUM THEORY FROM FIRST PRINCIPLES

An Informational Approach

GIACOMO MAURO D'ARIANO
GIULIO CHIRIBELLA
PAOLO PERINOTTI

CAMBRIDGE

Principles for Quantum Theory

P1. Causality

P2. Local discriminability

P3. Purification

P4. Atomicity of composition

P5. Perfect distinguishability

P6. Lossless Compressibility

G. Chiribella, G. M. D'Ariano, P. Perinotti, *Probabilistic Theories with Purification* Phys. Rev. A **81** 062348 (2010)

G. Chiribella, G. M. D'Ariano, P. Perinotti, *Informational derivation of Quantum Theory* Phys. Rev. A **84** 012311 (2011)

Principles for Quantum Theory

P1. **Causality**

P2. Local discriminability

P3. Purification

P4. Atomicity of composition

P5. Perfect distinguishability

P6. Lossless Compressibility

The probability of preparations is independent of the choice of observations



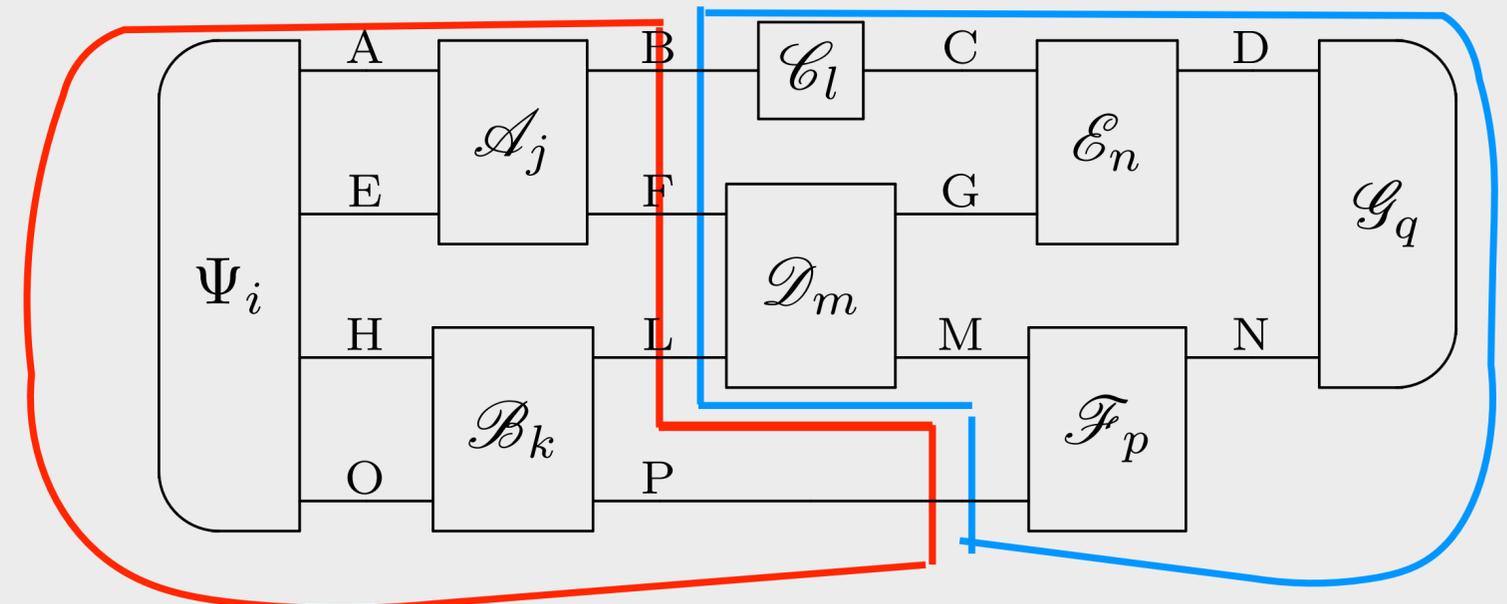
$$p(i, j | \mathcal{X}, \mathcal{Y}) := (a_j | \rho_i)$$



$$p(i | \mathcal{X}, \mathcal{Y}) = p(i | \mathcal{X}, \mathcal{Y}') = p(i | \mathcal{X})$$

Iff conditions: a) the deterministic effect is unique;
b) states are “normalizable”

$$p(i, j, k, l, m, n, p, q | \text{circuit})$$

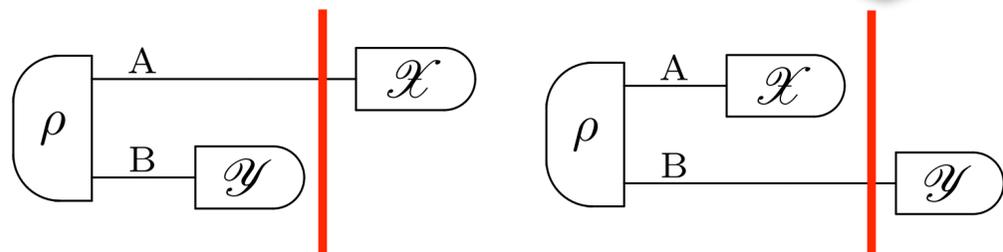


Principles for Quantum Theory

- P1. Causality
- P2. Local discriminability
- P3. Purification
- P4. Atomicity of composition
- P5. Perfect distinguishability
- P6. Lossless Compressibility

The probability of preparations is independent of the choice of observations

no signaling without interaction

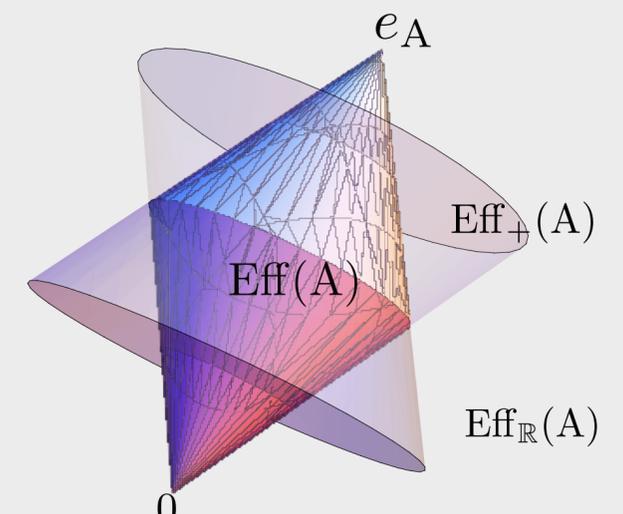
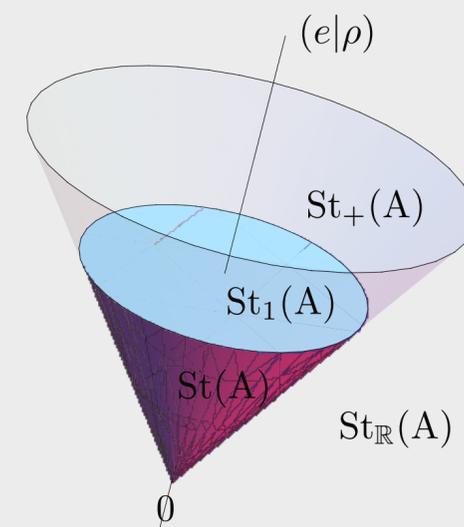
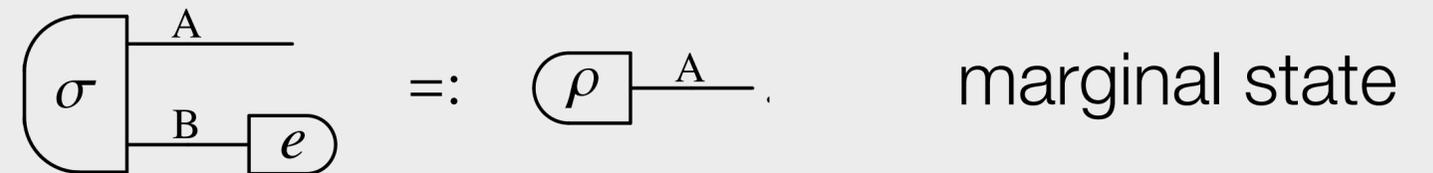


$$p(i, j | \mathcal{X}, \mathcal{Y}) := (a_j | \rho_i)$$



$$p(i | \mathcal{X}, \mathcal{Y}) = p(i | \mathcal{X}, \mathcal{Y}') = p(i | \mathcal{X})$$

Iff conditions: a) the deterministic effect is unique;
b) states are “normalizable”



Principles for Quantum Theory

P1. Causality

P2. Local discriminability

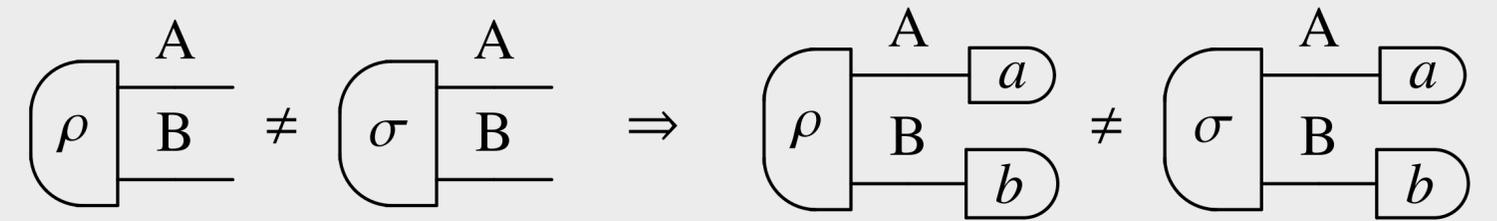
P3. Purification

P4. Atomicity of composition

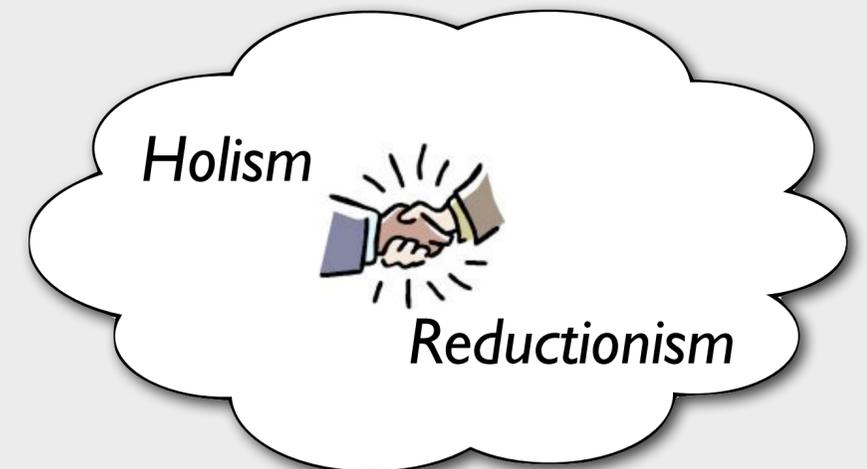
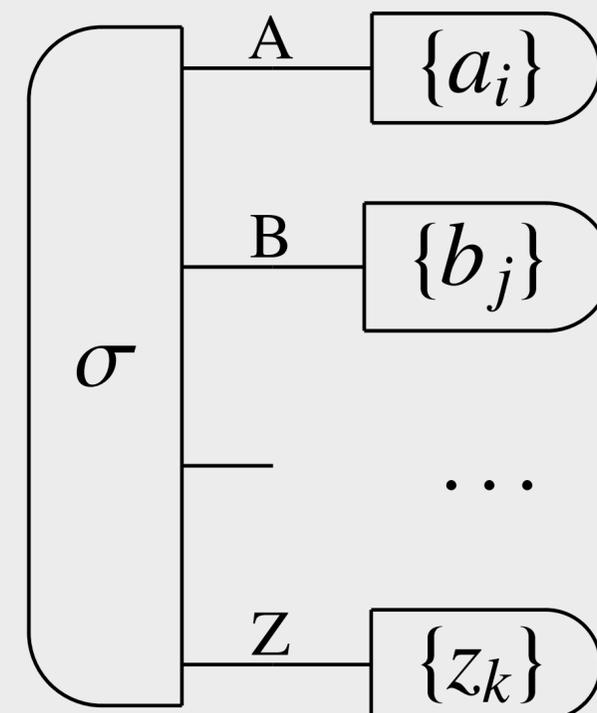
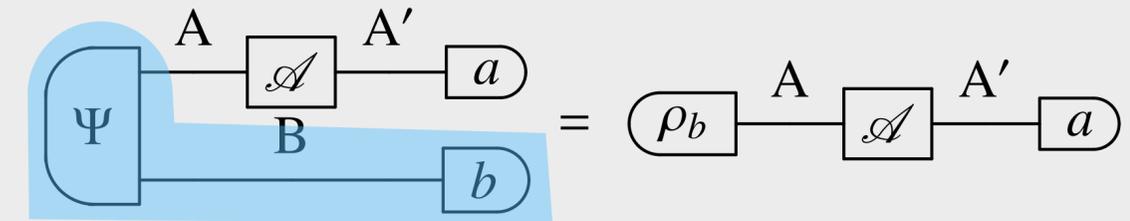
P5. Perfect distinguishability

P6. Lossless Compressibility

It is possible to discriminate any pair of states of composite systems using only local measurements.



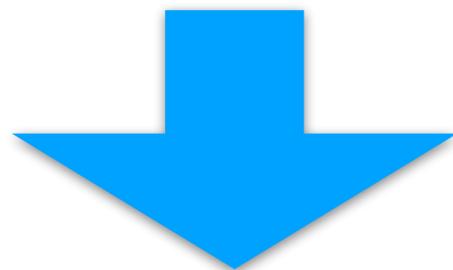
Local characterization of transformations



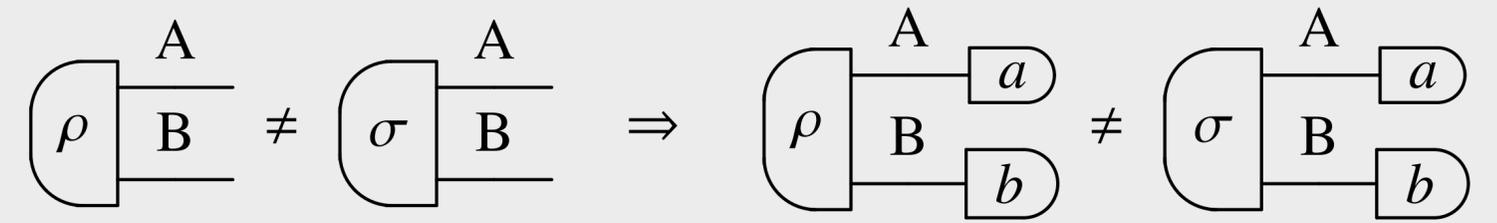
Principles for Quantum Theory

- P1. Causality
- P2. Local discriminability
- P3. Purification
- P4. Atomicity of composition
- P5. Perfect distinguishability
- P6. Lossless Compressibility

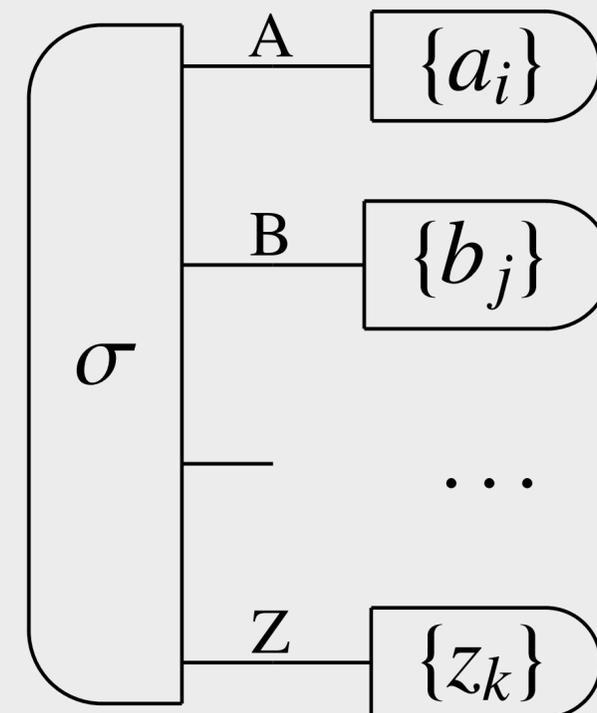
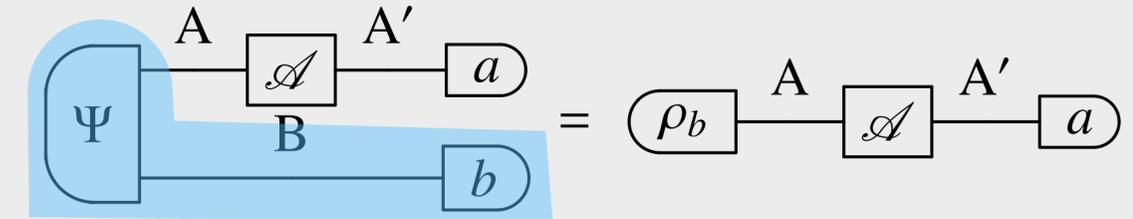
It is possible to discriminate any pair of states of composite systems using only local measurements.



Origin of the complex tensor product



Local characterization of transformations



Principles for Quantum Theory

P1. Causality

P2. Local discriminability

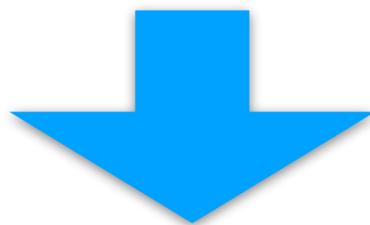
P3. Purification

P4. Atomicity of composition

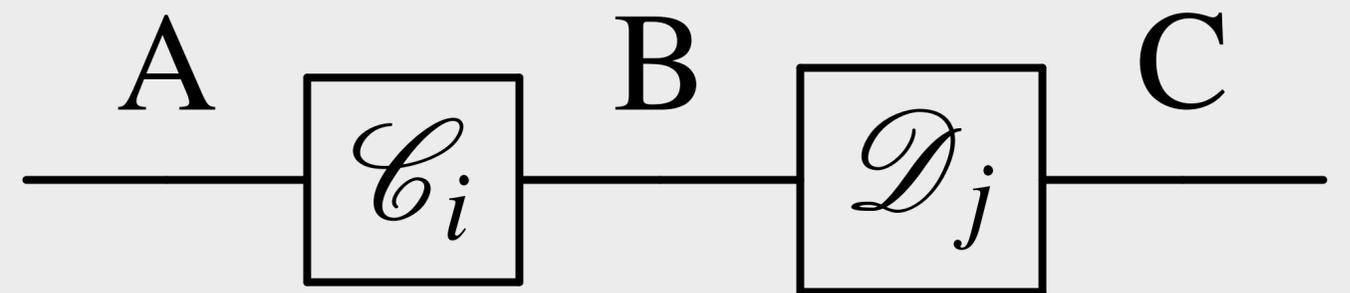
P5. Perfect distinguishability

P6. Lossless Compressibility

The composition of two atomic transformations is atomic



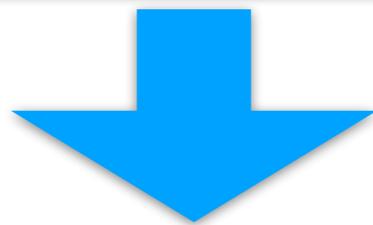
Complete information can be accessed
on a step-by-step basis



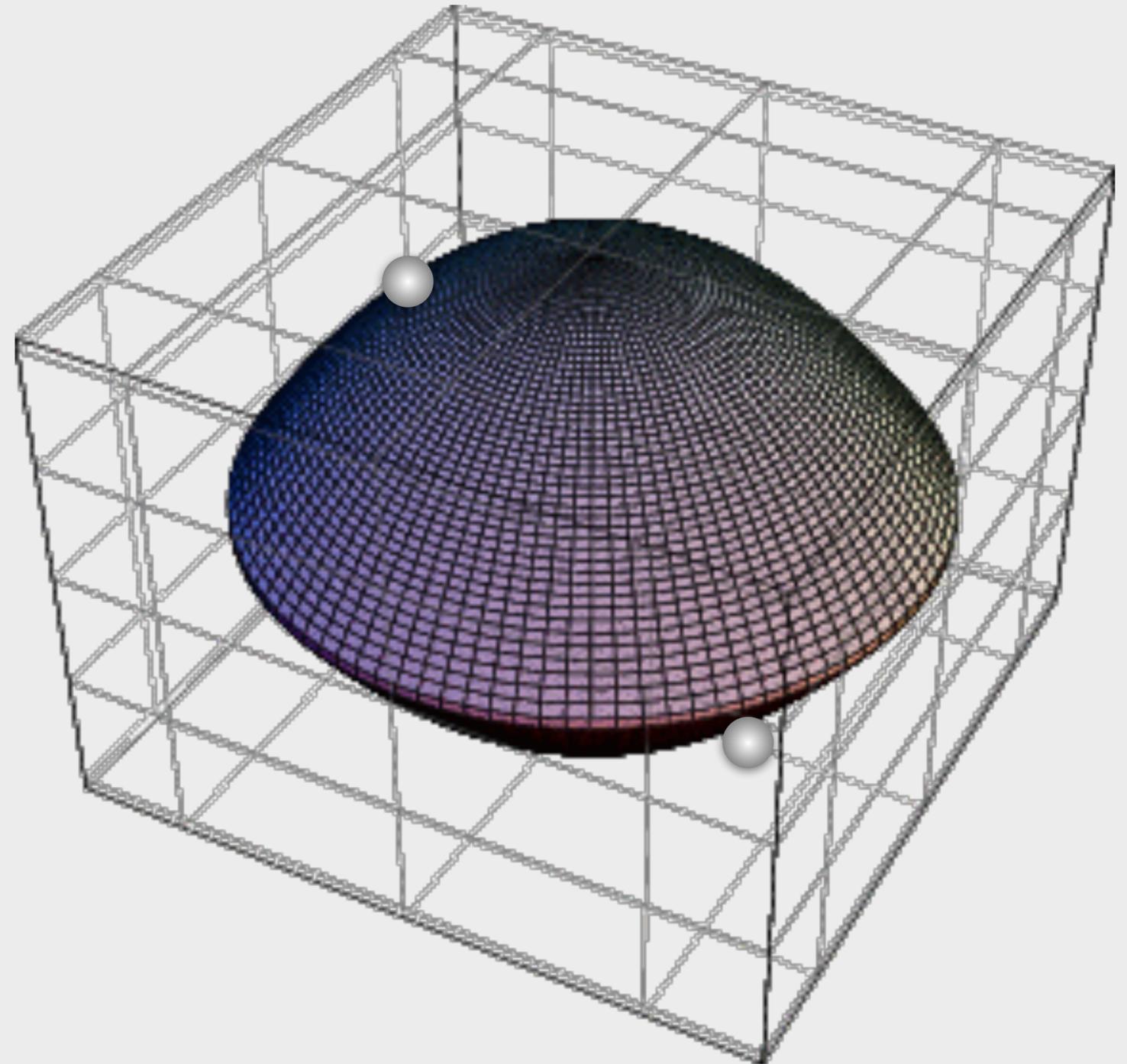
Principles for Quantum Theory

- P1. Causality
- P2. Local discriminability
- P3. Purification
- P4. Atomicity of composition
- P5. Perfect distinguishability
- P6. Lossless Compressibility

Every state that is not completely mixed (i.e. on the boundary of the convex) can be perfectly distinguished from some other state



Falsifiability of the theory

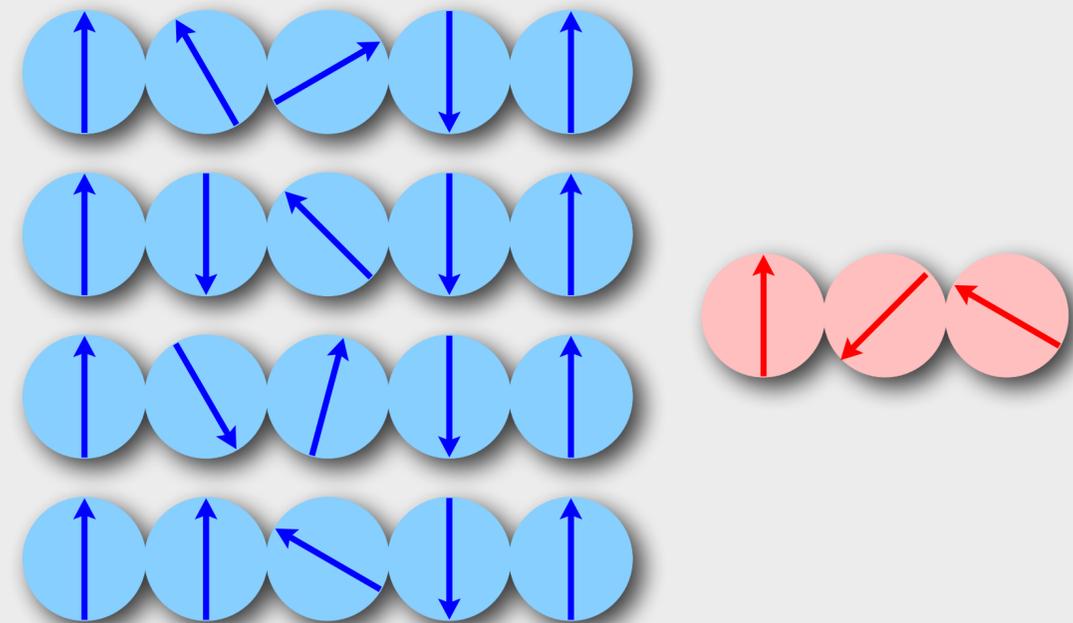
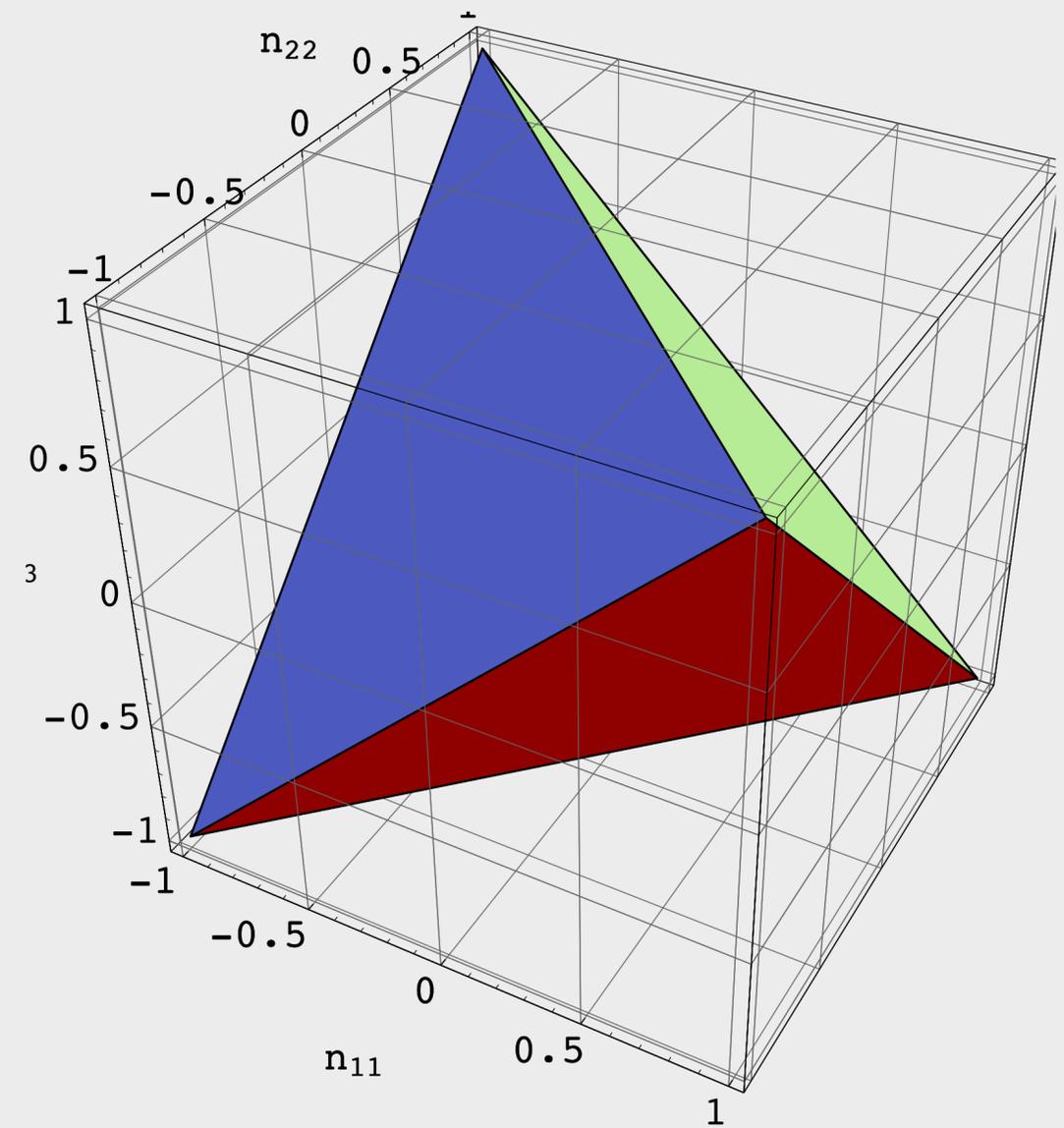


Principles for Quantum Theory

- P1. Causality
- P2. Local discriminability
- P3. Purification
- P4. Atomicity of composition
- P5. Perfect distinguishability
- P6. **Lossless Compressibility**

For states that are not completely mixed there exists an ideal compression scheme

Any face of the convex set of states is the convex set of states of some other system



Principles for Quantum Theory

P1. Causality

P2. Local discriminability

P3. Purification

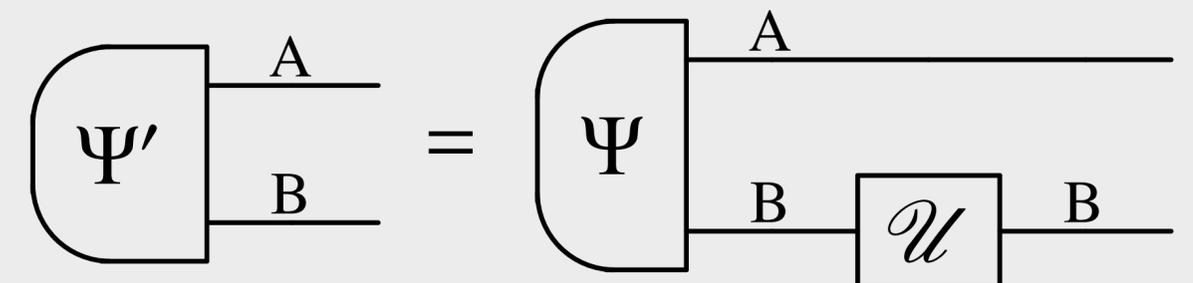
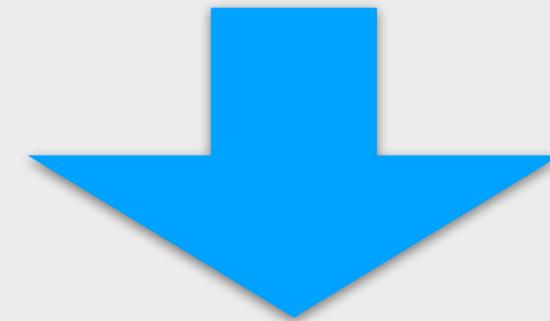
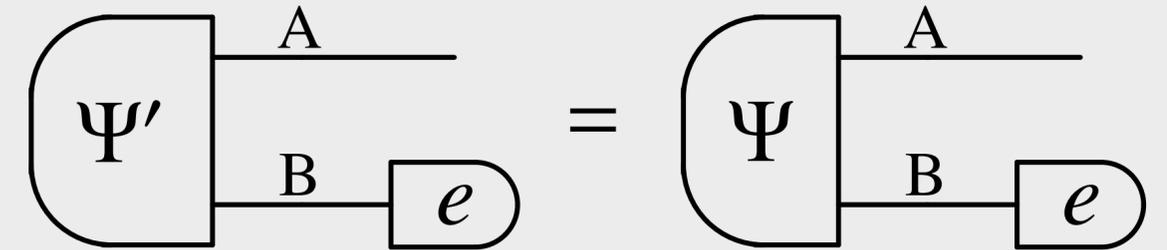
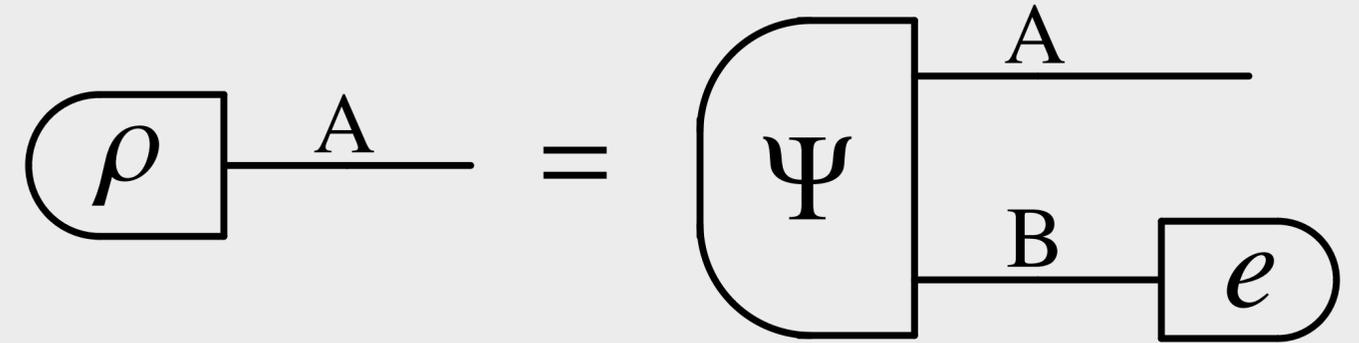
P4. Atomicity of composition

P5. Perfect distinguishability

P6. Lossless Compressibility

Every state has a purification.

For fixed purifying system, every two purifications of the same state are connected by a reversible transformation on the purifying system



Principles for Quantum Theory

P1. Causality

P2. Local discriminability

P3. Purification

P4. Atomicity of composition

P5. Perfect distinguishability

P6. Lossless Compressibility

Every state has a purification.

For fixed purifying system, every two purifications of the same state are connected by a reversible transformation on the purifying system

Consequences

1. Existence of entangled states:

the purification of a mixed state is an entangled state;
the marginal of a pure entangled state is a mixed state;

2. Every two normalized pure states of the same system are connected by a reversible transformation

$$\boxed{\psi'} \text{---}^B = \boxed{\psi} \text{---}^B \boxed{\mathcal{U}} \text{---}^B$$

3. Steering: Let Ψ purification of ρ . Then for every ensemble decomposition $\rho = \sum_x p_x \alpha_x$ there exists a measurement $\{b_x\}$, such that

$$\boxed{\Psi} \text{---}^A \text{---}^B \boxed{b_x} = p_x \boxed{\alpha_x} \text{---}^A \quad \forall x \in X$$

4. Process tomography (faithful state):

$$\boxed{\Psi} \text{---}^A \boxed{\mathcal{A}} \text{---}^{A'} = \boxed{\Psi} \text{---}^A \boxed{\mathcal{A}'} \text{---}^{A'} \quad \rightarrow \quad \mathcal{A}\rho = \mathcal{A}'\rho \quad \forall \rho$$

5. No information without disturbance

Principles for Quantum Theory

P1. Causality

P2. Local discriminability

P3. Purification

P4. Atomicity of composition

P5. Perfect distinguishability

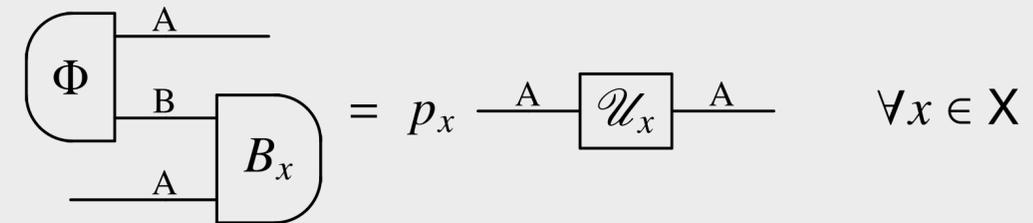
P6. Lossless Compressibility

Every state has a purification.

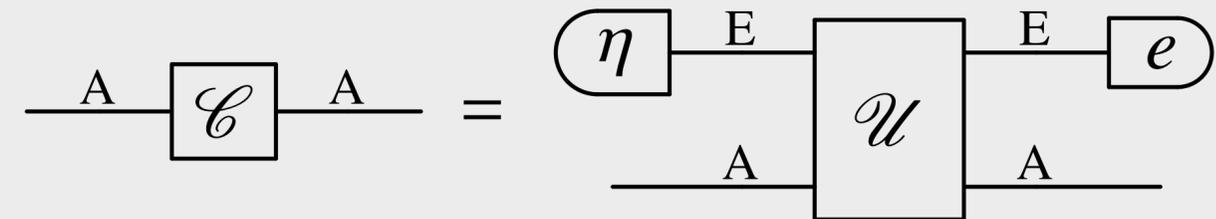
For fixed purifying system, every two purifications of the same state are connected by a reversible transformation on the purifying system

Consequences

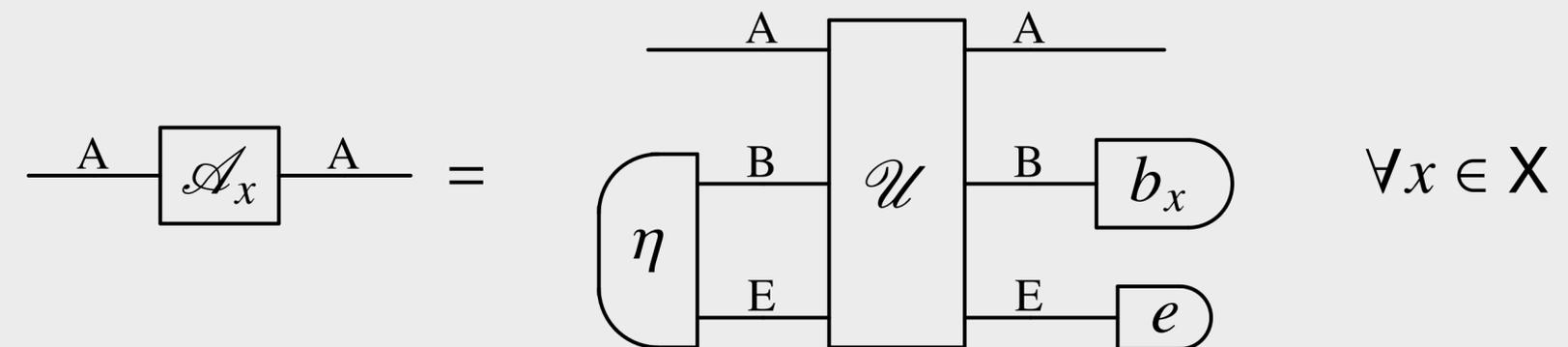
6. Teleportation



7. Reversible dilation of “channels”



8. Reversible dilation of “instruments”



9. State-transformation cone isomorphism

10. Reversible transform. for a system make a compact Lie group

Other OPTs

	Caus.	Perf. disc.	Loc. discr.	n-loc. discr.	At. par. comp.	At. seq. comp.	Compr.	\exists Purification	$\exists!$ Purification	NIWD
QT	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
CT	✓	✓	✓	✓	✓	✓	✓	✗	✗	✗
QBIT	✓	✓	✓	✓	✓	✓	✗	✓	✓	✓
FQT	✓	✓	✗	✓	✓	✓	✗	✓	✓	✓
RQT	✓	✓	✗	✓	✓	✓	✓	✓	✓	✓
NSQT	?	?	✗	✗	?	?	?	?	?	?
PR	✓	?	✓	✓	✓	?	✗	✗	✗	✓
DPR	✓	?	✓	✓	✓	?	✗	✗	✗	✓
HPR	✓	?	✓	✓	✓	✓	✓	✓	✓	✓
FOCT	✗	?	✓	✓	✓	?	?	✗	✗	?
FOQT	✗	?	?	✓	?	?	?	?	?	?
NLCT	✓	✓	✗	✓	✗	?	✓	✗	✗	✗
NLQT	?	?	?	✓	?	?	?	?	?	?

QT: Quantum theory

CT: Classical theory

QBIT: Qubit theory

FQT: Fermionic quantum theory

RQT: Real quantum theory

NSQT: Number superselected quantum theory

PR: PR-boxes theory

DPR: Dual PR-boxes theory

HPR: Hybrid PR-boxes theory

FOCT: First order classical theory

FOQT: First order quantum theory

NLCT: Non-local classical theory

NLQT: Non-local quantum theory

“HOW TO GET THE “MECHANICS?””

QUANTUM FIELD THEORY: an ultra-short account

PRINCIPLES

THEORY

RESTRICTIONS

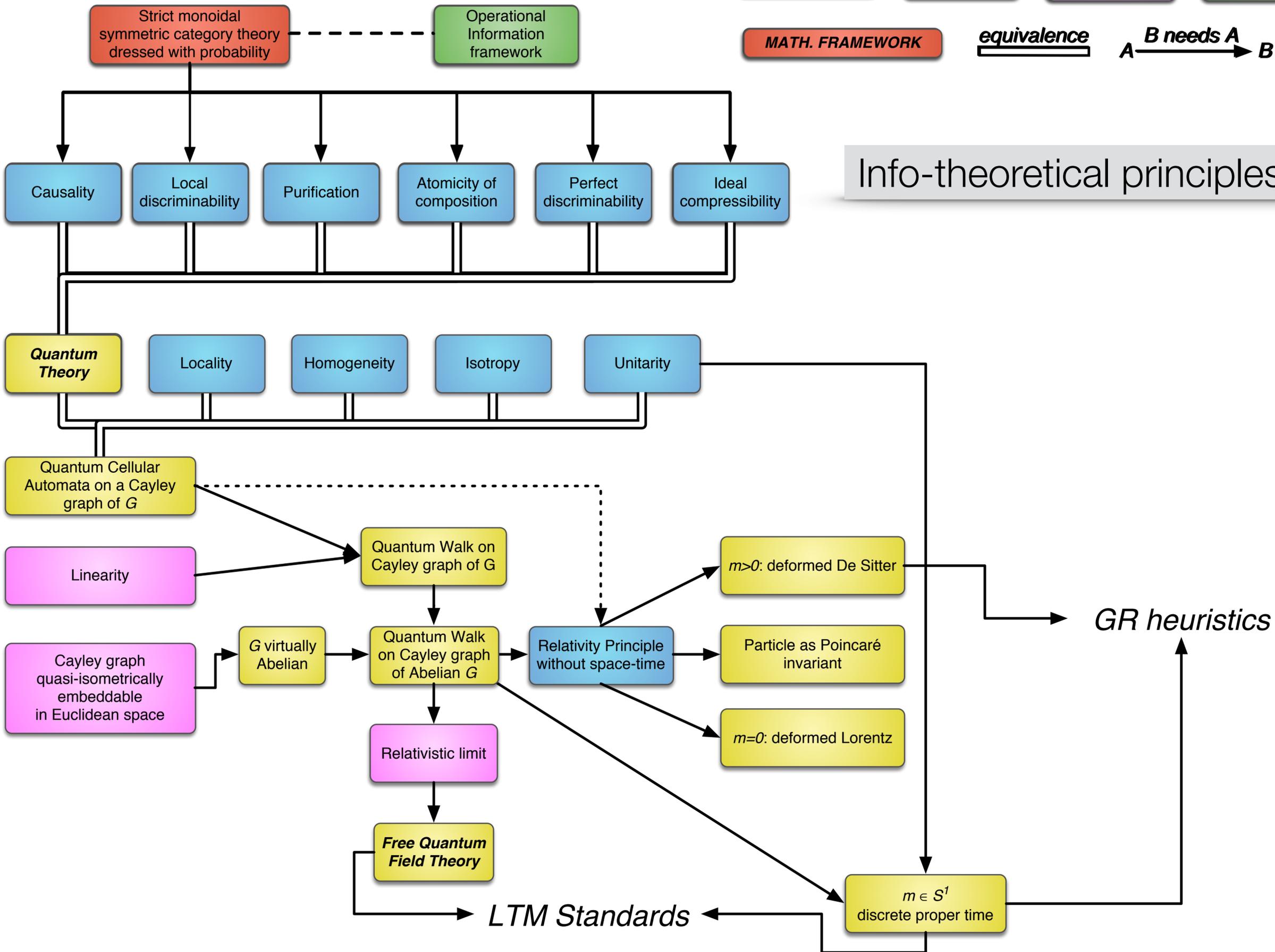
INTERPRETATION

MATH. FRAMEWORK

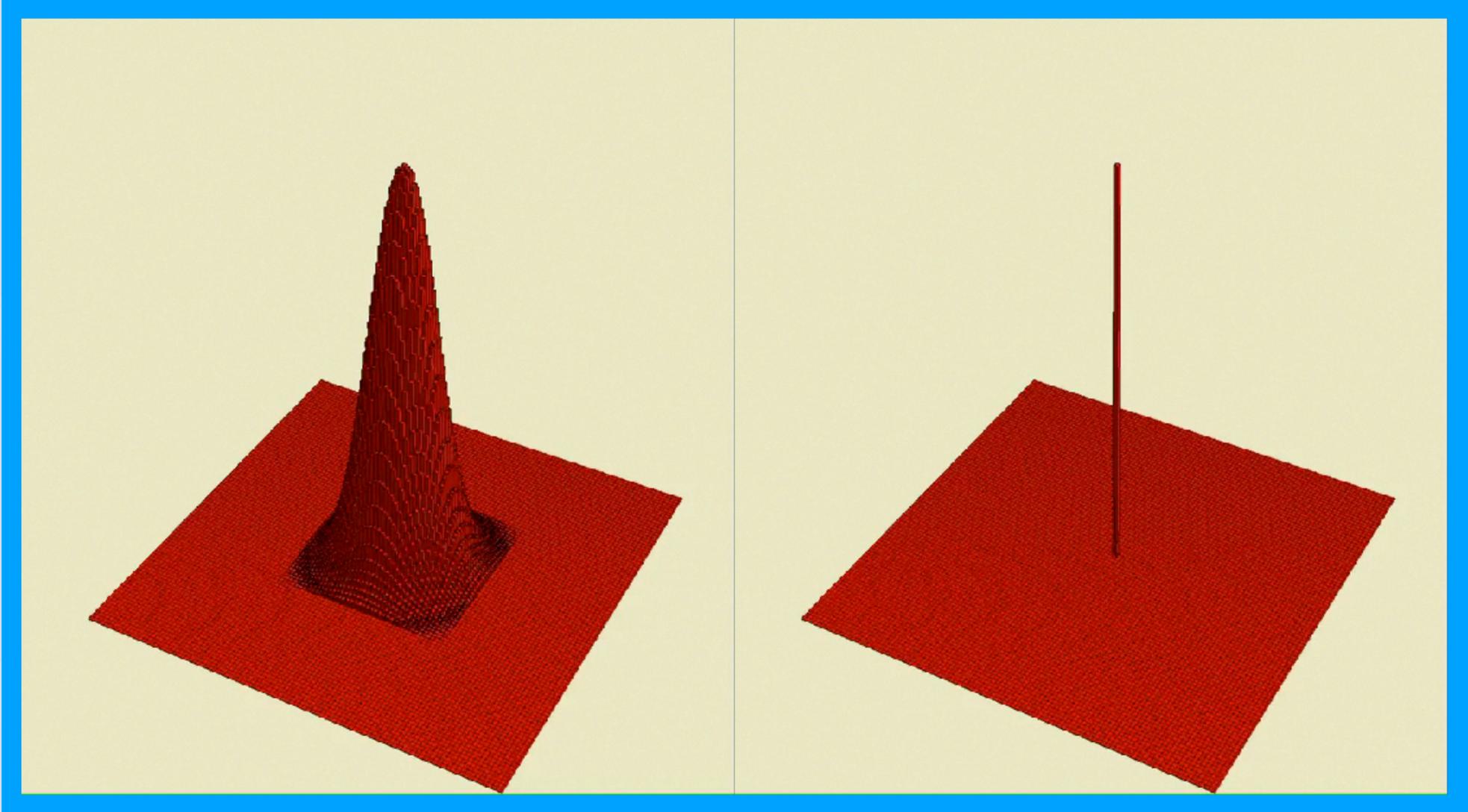
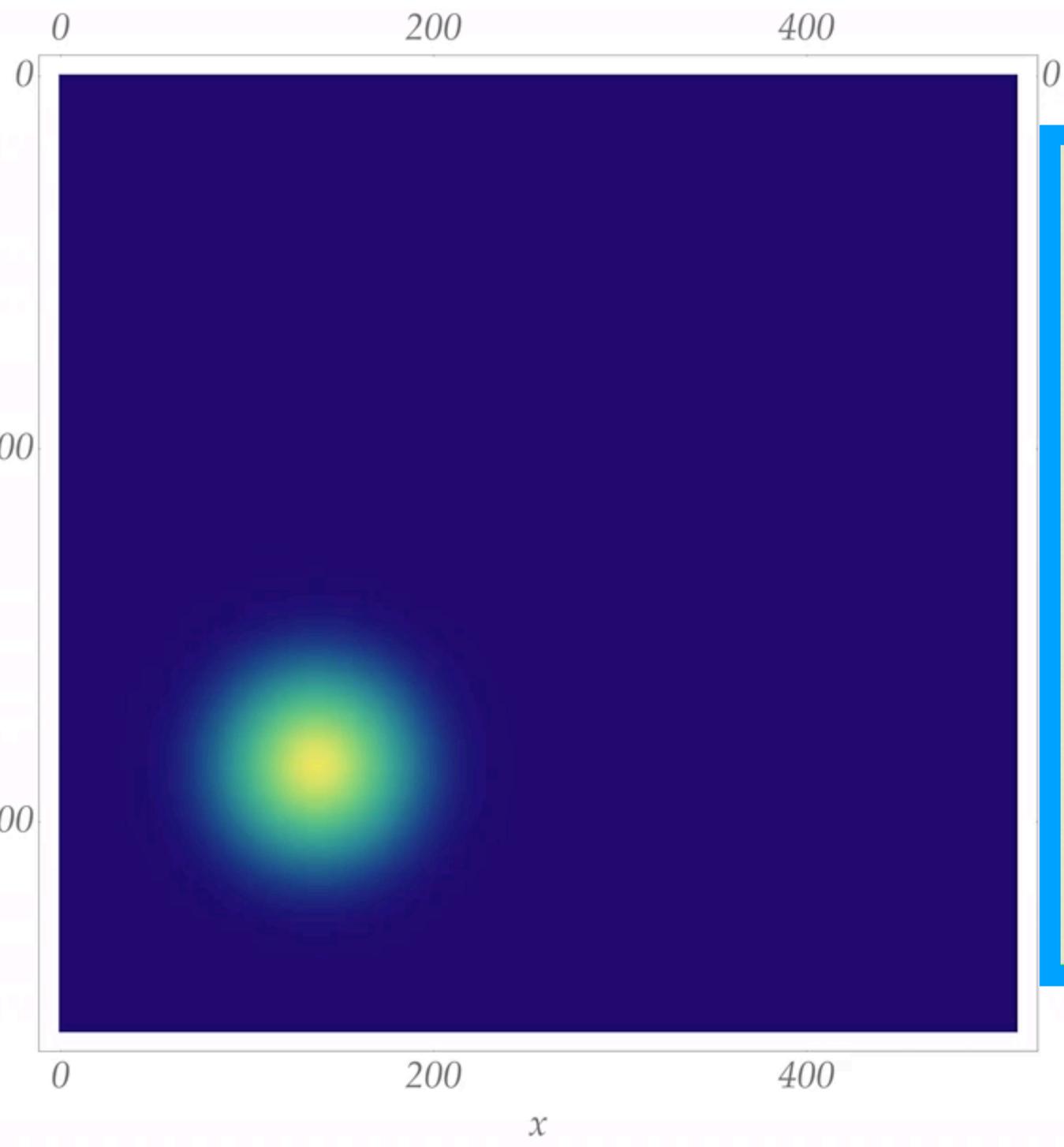
equivalence

$A \xrightarrow{B \text{ needs } A} B$

Info-theoretical principles for Quantum Field Theory



Info-theoretical principles for Quantum Field Theory



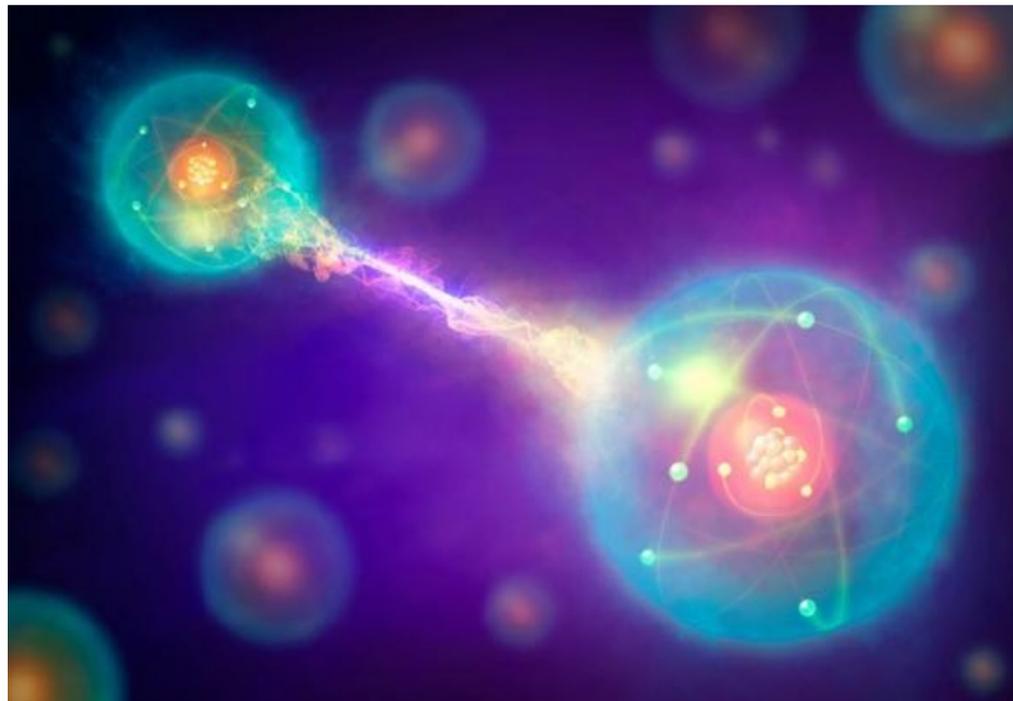
“NO PURIFICATION ONTOLOGY”

NO PARADOXES!

Quantum Theory: no purification ontology

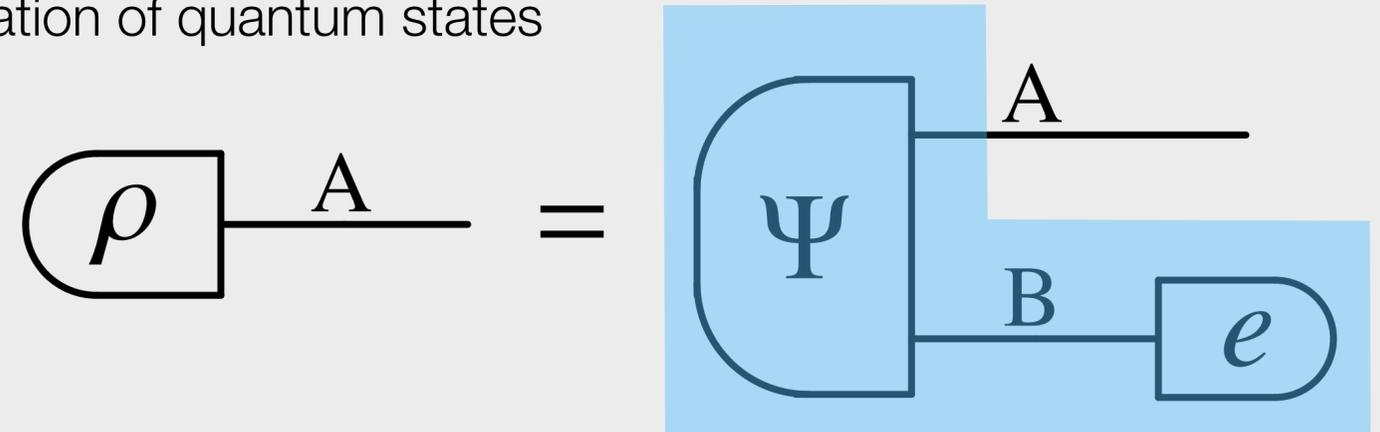
P3. Purification

1. Isolated systems don't need to be in a pure state!
2. Isolated systems don't need to undergo unitary transformations!

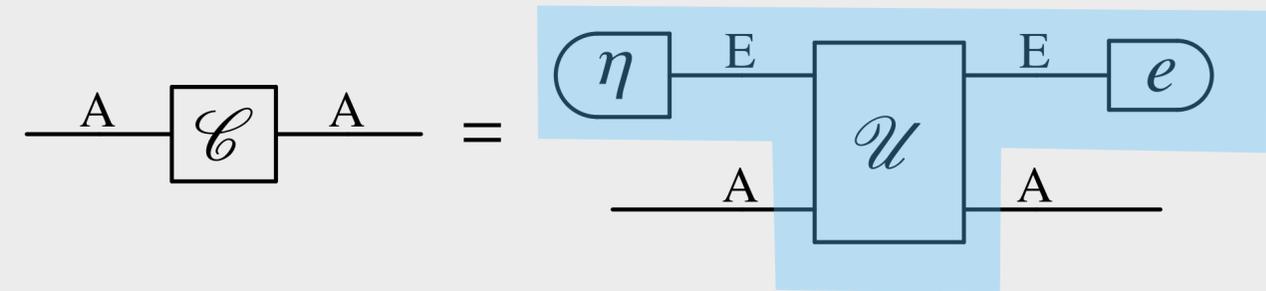


Unfalsifiable ontologies!

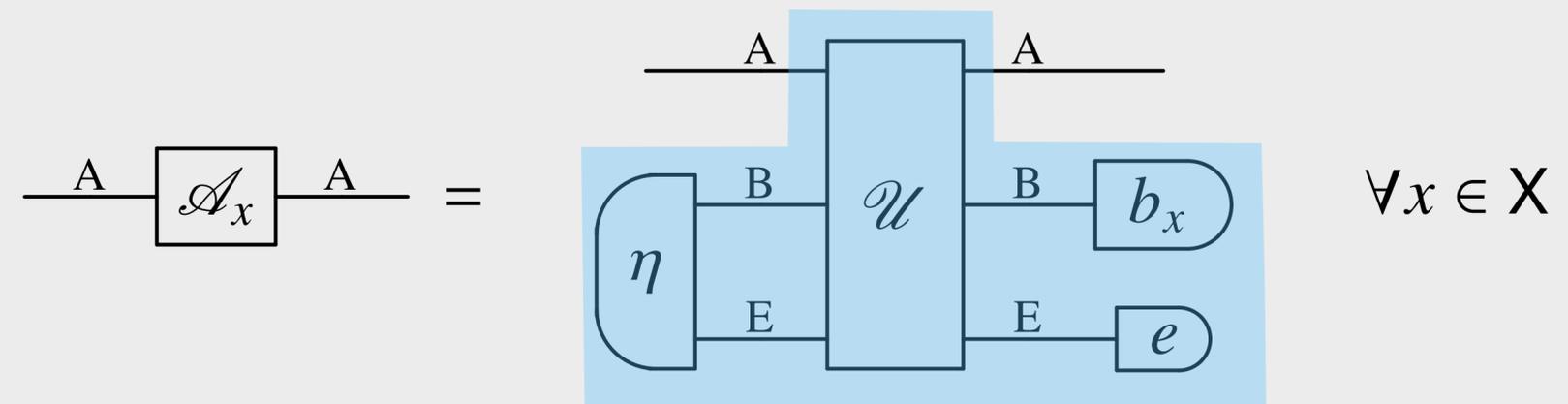
Purification of quantum states



Unitary purification of quantum channels



Unitary purification of quantum instruments



Quantum Theory: no purification ontology

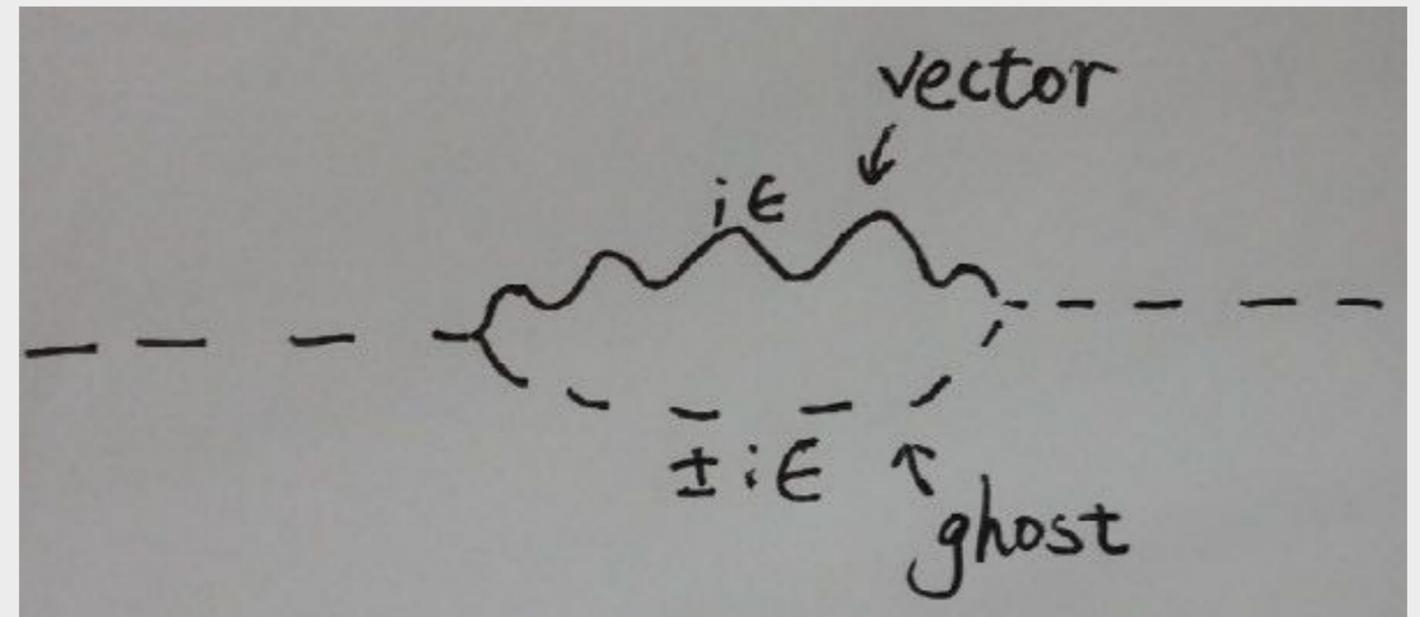
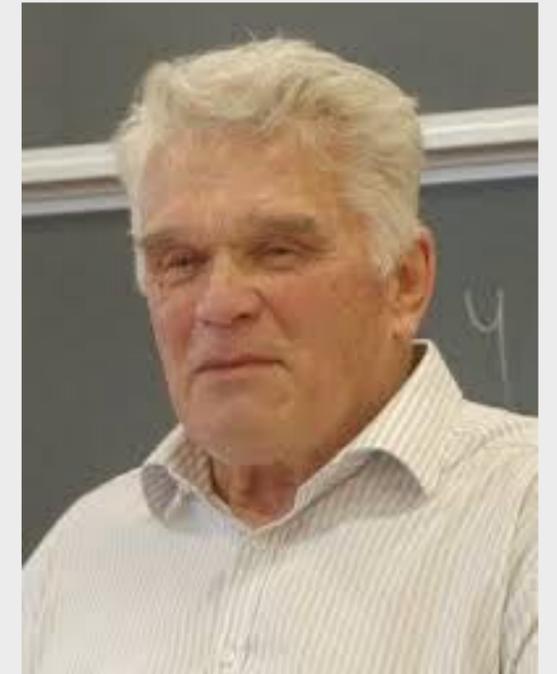
P3. Purification

1. Isolated systems don't need to be in a pure state
2. Isolated systems don't need to undergo unitary transformations

The necessity for Faddeev–Popov ghosts follows from the requirement that quantum field theories yield unambiguous, non-singular solutions. This is not possible in the path integral formulation when a gauge symmetry is present since there is no procedure for selecting among physically equivalent solutions related by gauge transformation. The path integrals overcount field configurations corresponding to the same physical state; the measure of the path integrals contains a factor which does not allow obtaining various results directly from the action.

It is possible, however, to modify the action, such that methods such as Feynman diagrams will be applicable by adding ghost fields which break the gauge symmetry. **The ghost fields do not correspond to any real particles in external states: they appear as virtual particles in Feynman diagrams – or as the absence of gauge configurations. However, they are a necessary computational tool to preserve unitarity.**

Unitarity in quantum field theory?



“Angel” of the Theory



A theoretical notion that:

- can achieve elements of the theory (powerful)
- is logically coherent within the theory
- is non falsifiable in principle
- is unnecessary for completeness of the theory



A theoretical notion that:

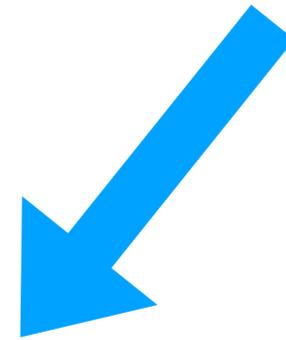
- can achieve elements of the theory (powerful)
- is logically coherent within the theory
- is non falsifiable in principle
- is not necessary for completeness of the theory

PURIFICATIONS
(UNITARITY and PURITY)
are ANGELS of QT

(the purification postulate, however, is in principle falsifiable)



Academical distinction



Quantum Theory

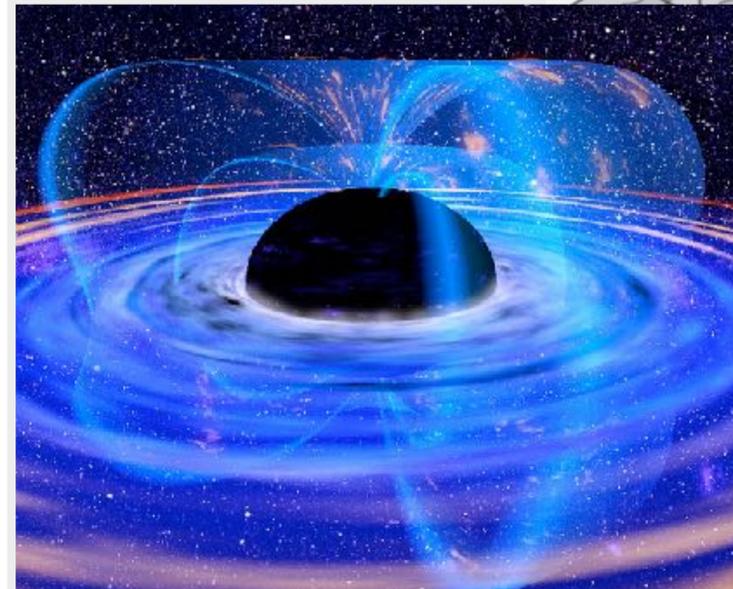
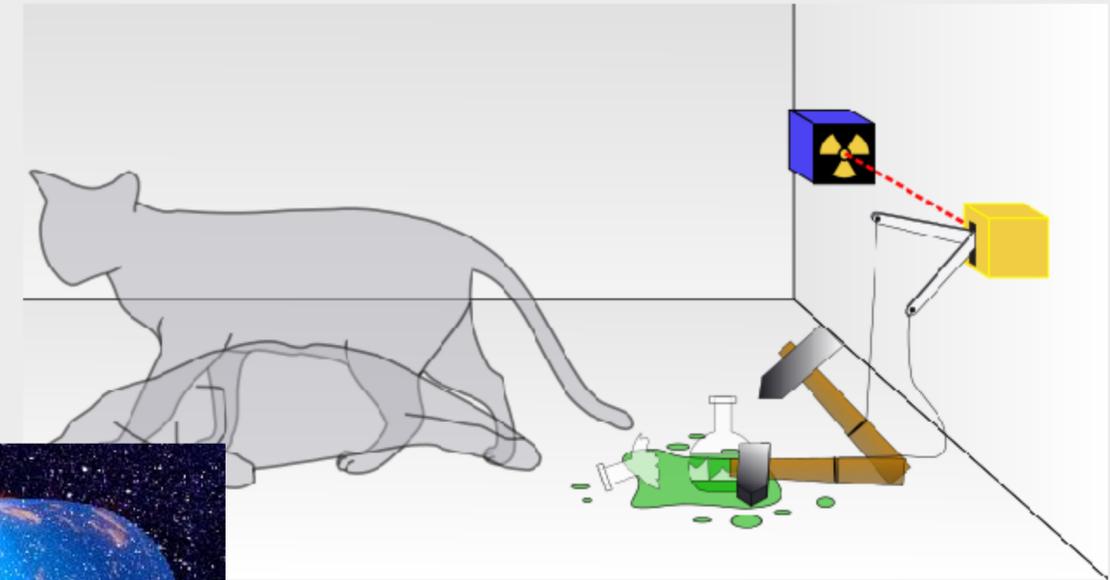
Open Quantum Systems Theory

Quantum Theory: no purification ontology

1. Isolated systems don't need to be in a pure state
2. Isolated systems don't need to undergo unitary transformations

No paradoxes, and more ...

Schroedinger's cat



Information paradox

Many-world,
relational, ...
interpretations



Wheeler-DeWitt
equation

$$H(x) |\psi\rangle = 0$$



Purification is a “symmetry”

Can we find a substitute?

**This is more or less
what I wanted to say**

THANK YOU!

A Quantum-Digital Universe, Grant ID: 43796
Quantum Causal Structures, Grant ID: 60609

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deriving the whole physics from information-theoretical principles.*



REVIEW

G. M. D'Ariano, *Physics without Physics*, Int. J. Theor. Phys. **128** 56 (2017),
[in memoriam of D. Finkelstein]

OPINION
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G.M. D'Ariano, *Causality re-established*, Phil. Trans. R. Soc. A **376**: 20170313 (2018)

The solution of the Sixth Hilbert Problem: the Ultimate Galilean Revolution, Phil. Trans. R. Soc. A **376**: 20170224 (2018)